



# Encoding and Decoding 3-D Crystals

Jordan Hoffmann · Louis Maestrati · Yoshihide Sawada  
Jian Tang · Jean Michel Sellier · Yoshua Bengio

# Applications

Specific compounds of interest:

- batteries
- solar cells

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Targeted

(Now) Works well for drug discovery.

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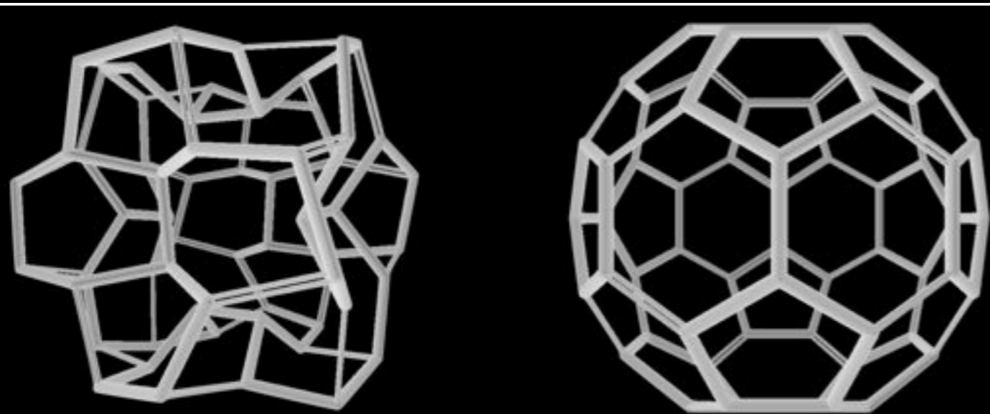
Targeted

(Now) Works well for drug discovery.

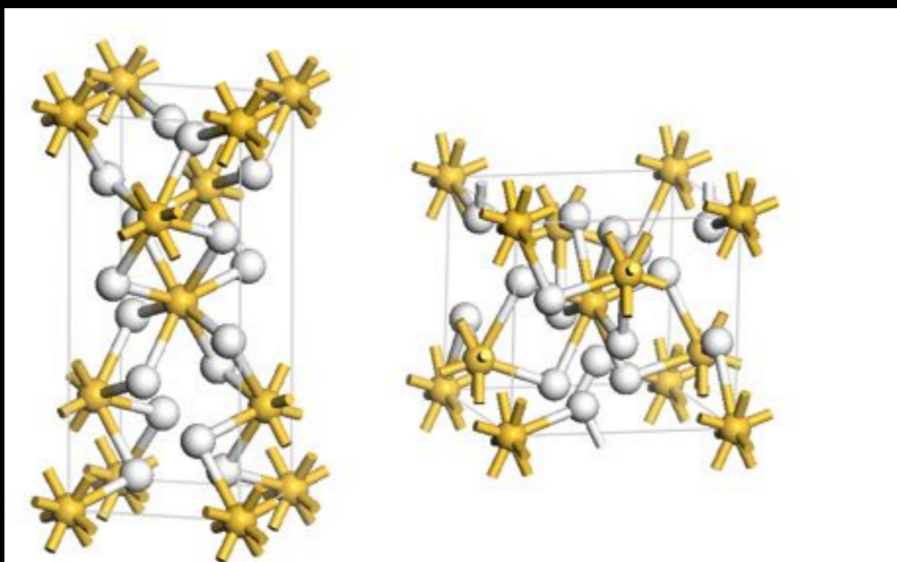
## Random structure searching

### Abstract

It is essential to know the arrangement of the atoms in a material in order to compute and understand its properties. Searching for stable structures of materials using first-principles electronic structure methods, such as density-functional-theory (DFT), is a rapidly growing field. Here we describe our simple, elegant and powerful approach to searching for structures with DFT, which we call *ab initio* random structure searching (AIRSS). Applications to discovering the structures of solids, point defects, surfaces, and clusters are reviewed. New results for iron clusters on graphene, silicon clusters, polymeric nitrogen, hydrogen-rich lithium hydrides, and boron are presented.



**Figure 3.** Left: A structure built by placing carbon atoms randomly within a small sub-box, subject to symmetry constraints. Random structures were generated and then screened to determine whether the atoms were three-fold coordinated. If not, the structure was rejected and another one was generated. Right: relaxation of this structure within DFT gave the well-known  $C_{60}$  “buckyball”.

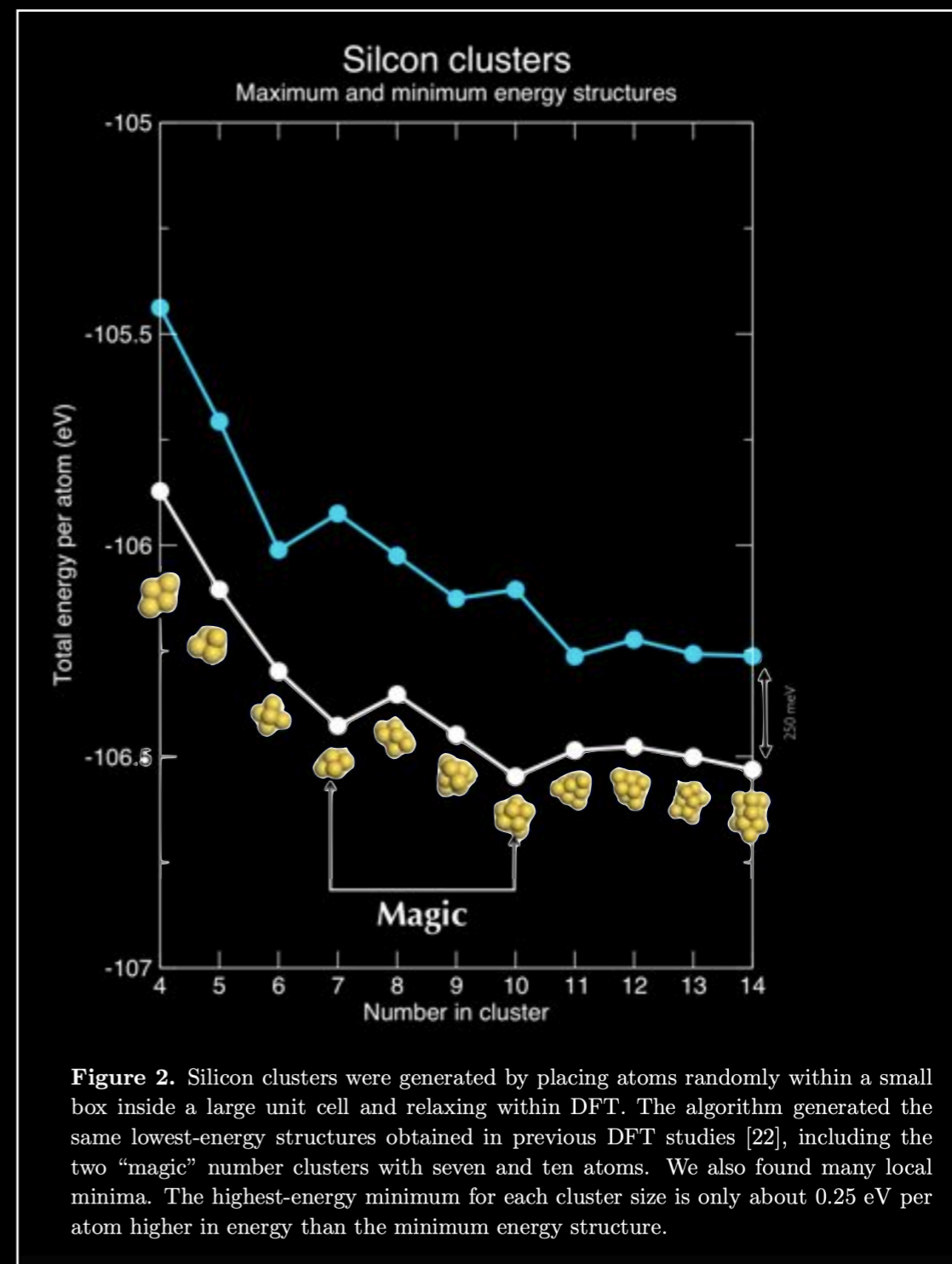


**Figure 8.** The  $I4_1/a$  structure of silane (left) and the slightly less stable  $I\bar{4}2d$  structure (right). Silicon atoms are shown in gold and hydrogen atoms are in white. All of the bonds in  $I4_1/a$  and  $I\bar{4}2d$  are of the Si-H-Si type. Both phases were subsequently found experimentally.

## High-Pressure Phases of Silane

Chris J. Pickard and R. J. Needs

Phys. Rev. Lett. **97**, 045504 – Published 27 July 2006



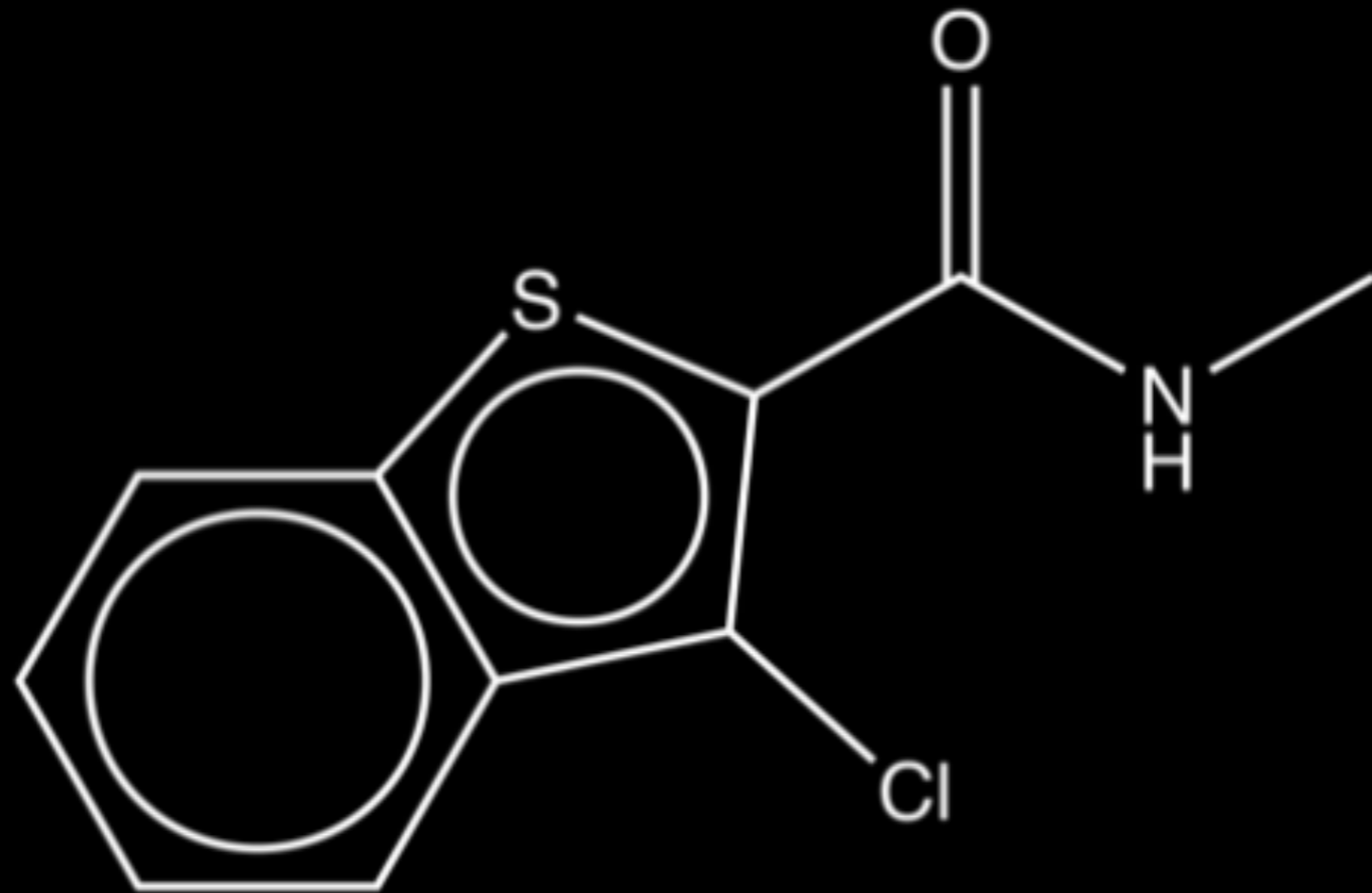
**Figure 2.** Silicon clusters were generated by placing atoms randomly within a small box inside a large unit cell and relaxing within DFT. The algorithm generated the same lowest-energy structures obtained in previous DFT studies [22], including the two “magic” number clusters with seven and ten atoms. We also found many local minima. The highest-energy minimum for each cluster size is only about 0.25 eV per atom higher in energy than the minimum energy structure.

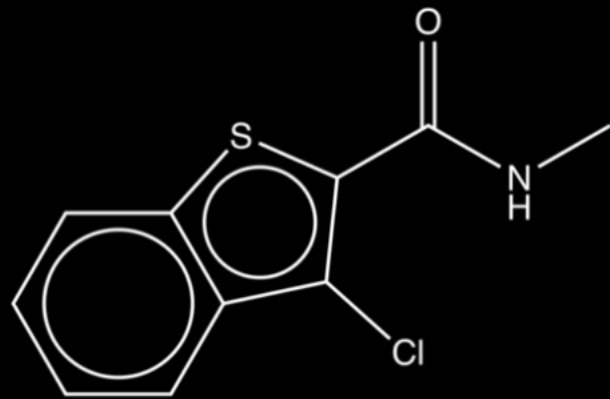
## *Ab initio* random structure searching

Chris J Pickard<sup>1</sup> and R J Needs<sup>2</sup>

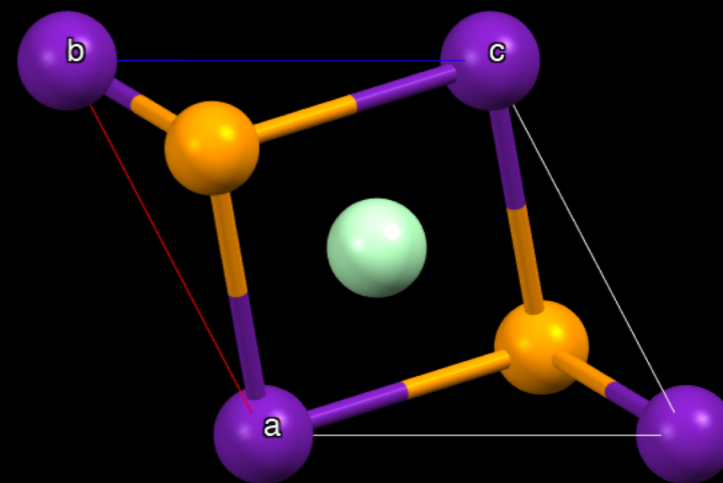
Published 5 January 2011 • IOP Publishing Ltd

[Journal of Physics: Condensed Matter](#), Volume 23, Number 5





Drug-like Molecule



Crystal Structure

SMILES string Cn1cnc2n(C)c(=O)n(C)c(=O)c12



Not applicable

Graph representation



Need location information

Tend to use 5-20 total atoms



Tend to use 1-100 total atoms

Mostly C,H,O- less than 10 total species

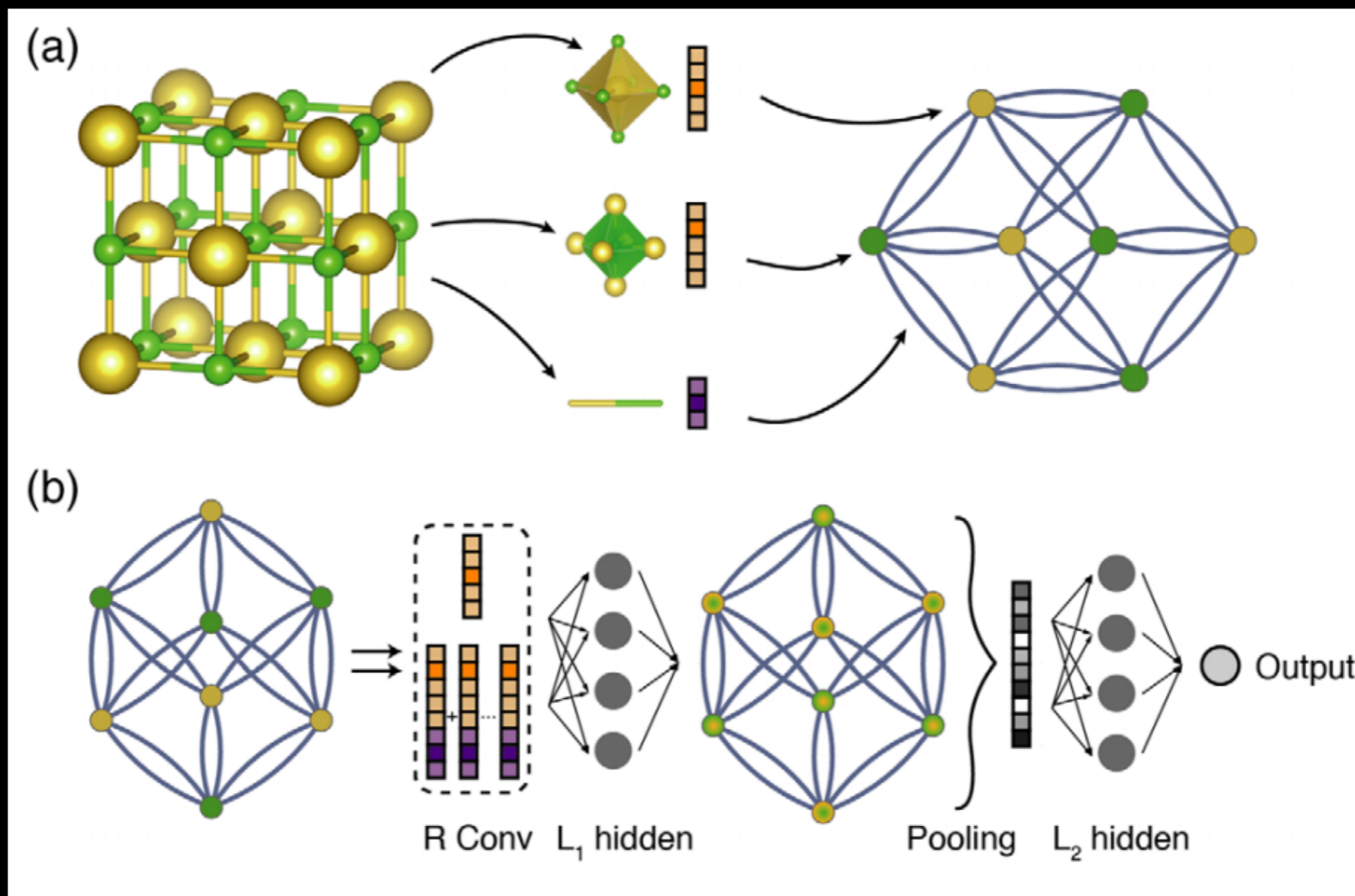


Entire periodic table

Less data exists  
slower to compute

6 additional degrees of freedom  
are needed





# Crystal Graph Convolutional Neural Networks for an Accurate and Interpretable Prediction of Material Properties

Tian Xie and Jeffrey C. Grossman

Phys. Rev. Lett. **120**, 145301 – Published 6 April 2018

# Input format

```
1 # generated using pymatgen
2 data_Ti2MnIn
3 _symmetry_space_group_name_H-M 'P 1'
4 _cell_length_a 4.48903651
5 _cell_length_b 4.48903651
6 _cell_length_c 4.48903651
7 _cell_angle_alpha 60.00000000
8 _cell_angle_beta 60.00000000
9 _cell_angle_gamma 60.00000000
10 _symmetry_Int_Tables_number 1
11 _chemical_formula_structural Ti2MnIn
12 _chemical_formula_sum 'Ti2 Mn1 In1'
13 _cell_volume 63.96529632
14 _cell_formula_units_Z 1
15 loop_
16 _symmetry_equiv_pos_site_id
17 _symmetry_equiv_pos_as_xyz
18 1 'x, y, z'
19 loop_
20 _atom_site_type_symbol
21 _atom_site_label
22 _atom_site_symmetry_multiplicity
23 _atom_site_fract_x
24 _atom_site_fract_y
25 _atom_site_fract_z
26 _atom_site_occupancy
27 Ti Ti1 1 -0.000000 0.000000 0.000000 1
28 Ti Ti2 1 0.750000 0.750000 0.750000 1
29 Mn Mn3 1 0.500000 0.500000 0.500000 1
30 In In4 1 0.250000 0.250000 0.250000 1
```

We need:

- 1.) Locations
- 2.) Species

$$M_{i,j,k} = \frac{1}{\sigma^3 (2\pi)^{3/2}} \sum_m Z_m \exp \left( -\frac{d(\vec{Z}_m, (i, j, k))^2}{2\sigma^2} \right)$$

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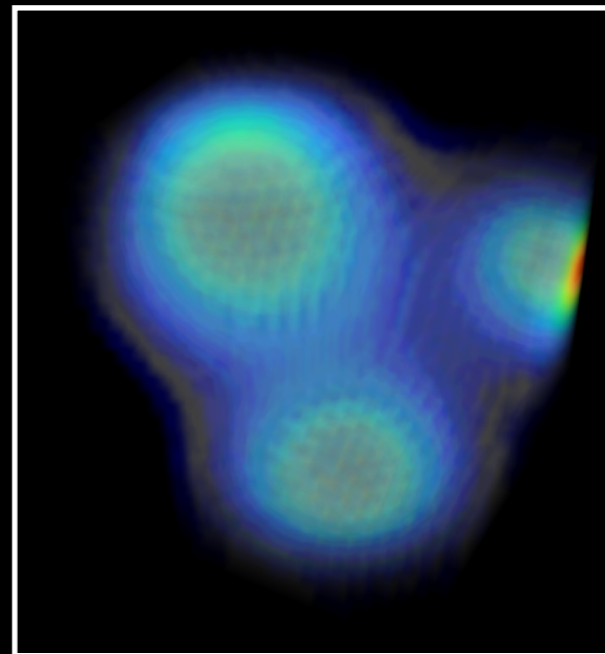
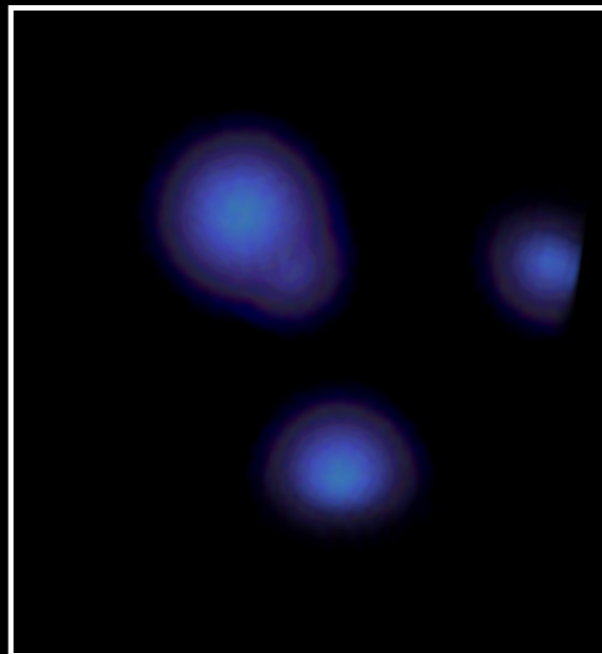
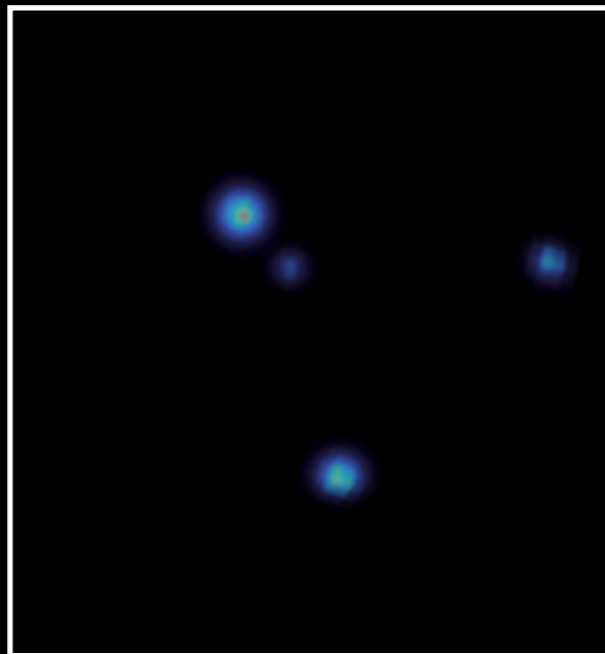
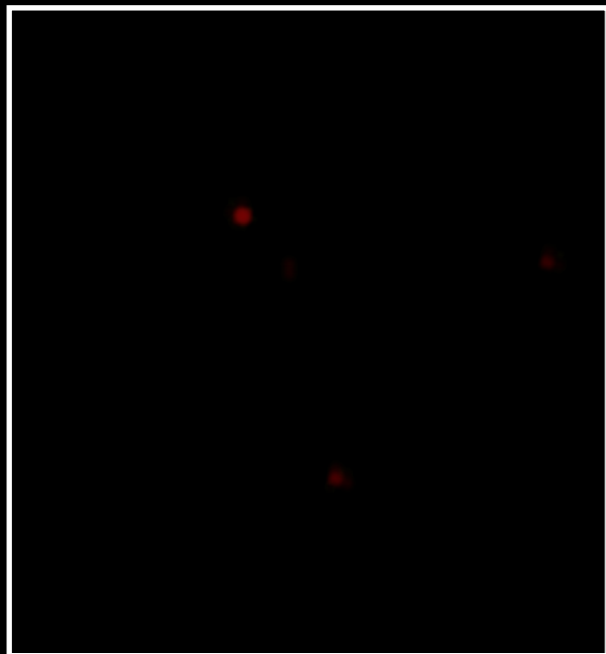
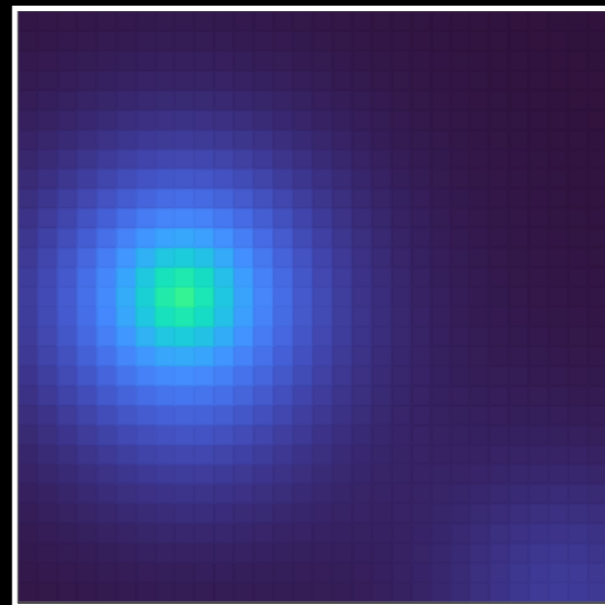
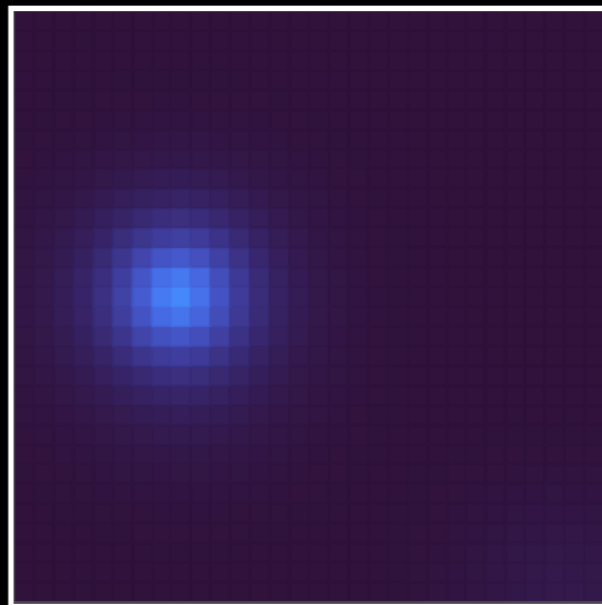
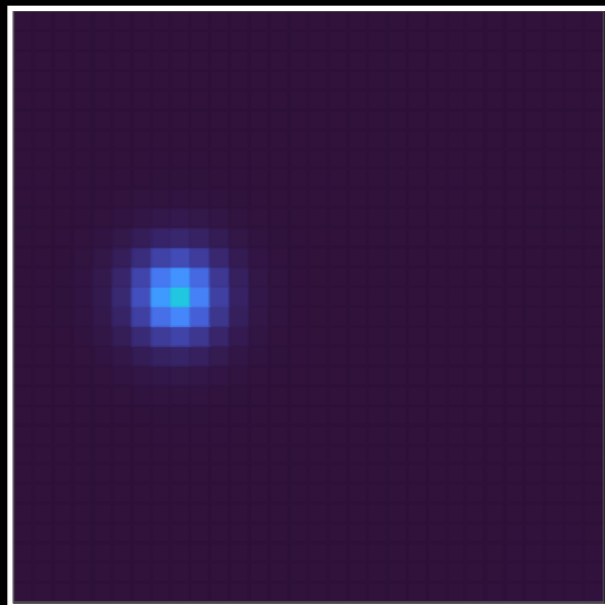
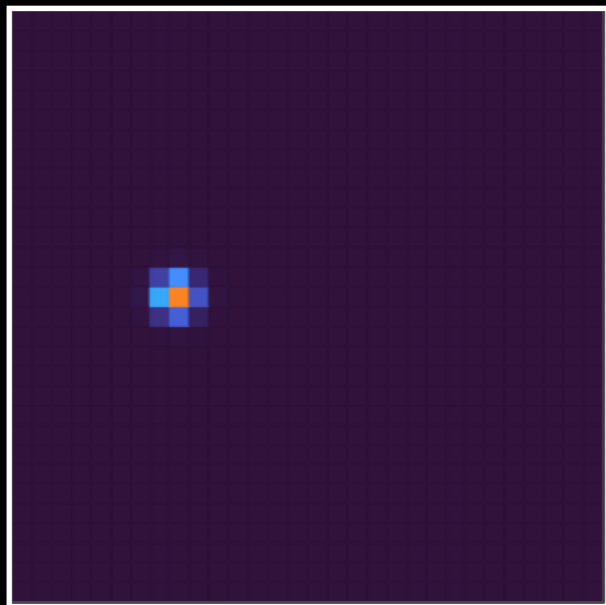
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7 _cell_angle_alpha 60.00000000
8 _cell_angle_beta 60.00000000
9 _cell_angle_gamma 60.00000000
10 _symmetry_Int_Tables_number 1
11 _chemical_formula_structural Ti2MnIn
12 _chemical_formula_sum 'Ti2 Mn1 In1'
13 _cell_volume 63.96529632
14 _cell_formula_units_Z 1
15 loop_
16 _symmetry_equiv_pos_site_id
17 _symmetry_equiv_pos_as_xyz
18 1 'x, y, z'
19 loop_
20 _atom_site_type_symbol
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22 _atom_site_symmetry_multiplicity
23 _atom_site_fract_x
24 _atom_site_fract_y
25 _atom_site_fract_z
26 _atom_site_occupancy
27 Ti Ti1 1 -0.000000 0.000000 0.000000 1
28 Ti Ti2 1 0.750000 0.750000 0.750000 1
29 Mn Mn3 1 0.500000 0.500000 0.500000 1
30 In In4 1 0.250000 0.250000 0.250000 1

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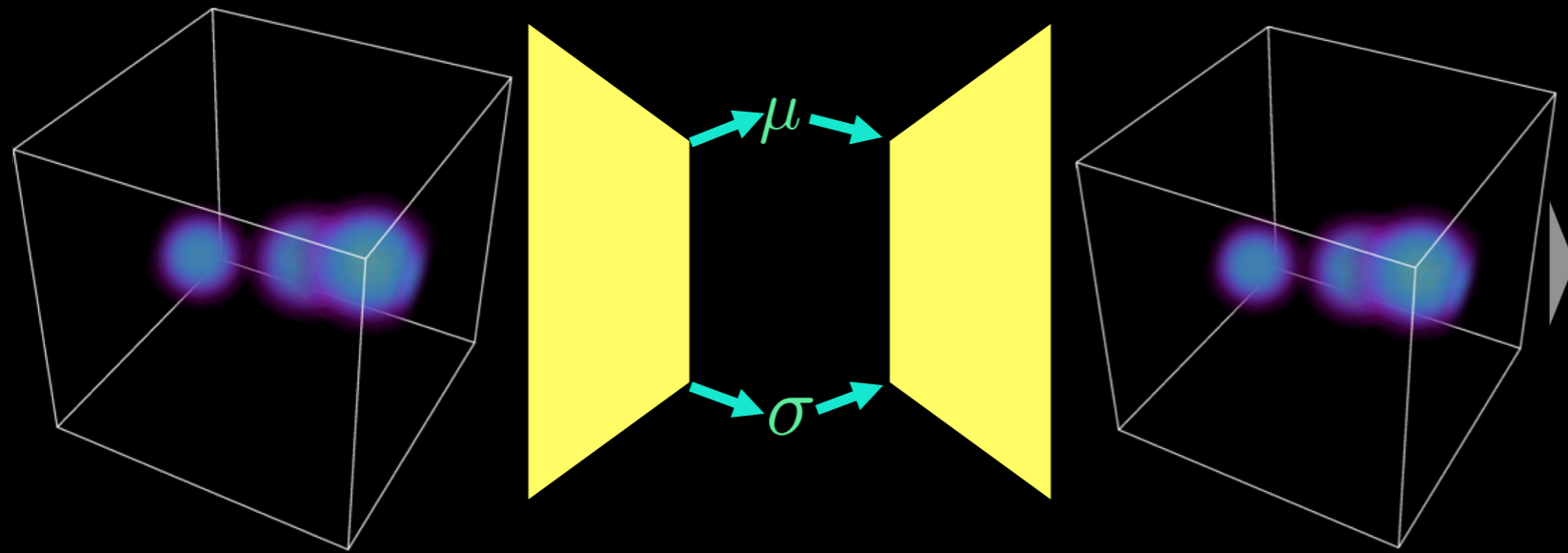
$$\mathbf{M}_{i,j,k} = \frac{1}{\sigma^3 (2\pi)^{3/2}} \sum_m \mathbf{Z}_m \exp \left( -\frac{d(\vec{\mathbf{Z}}_m, (i, j, k))^2}{2\sigma^2} \right)$$

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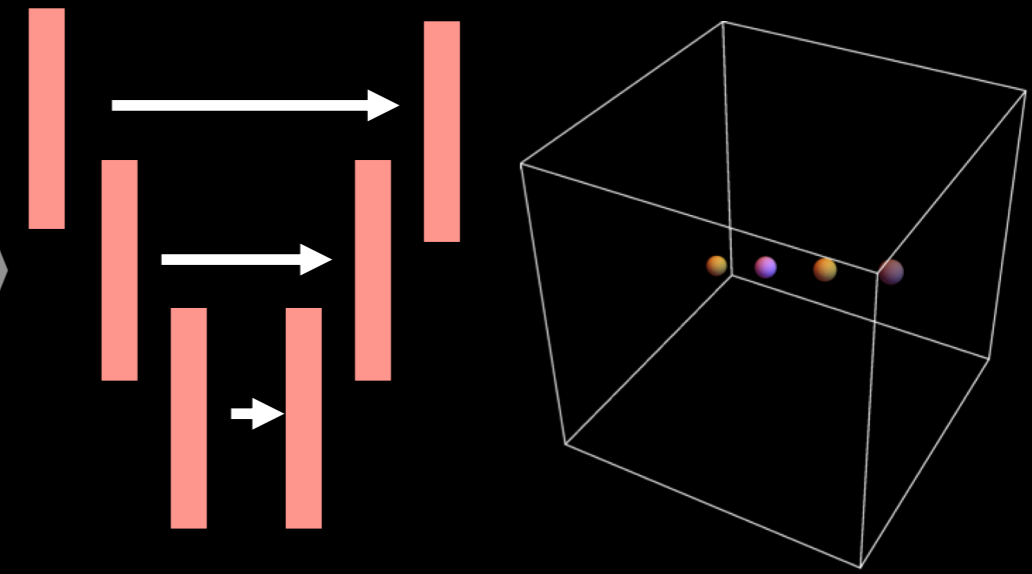
$\sigma$



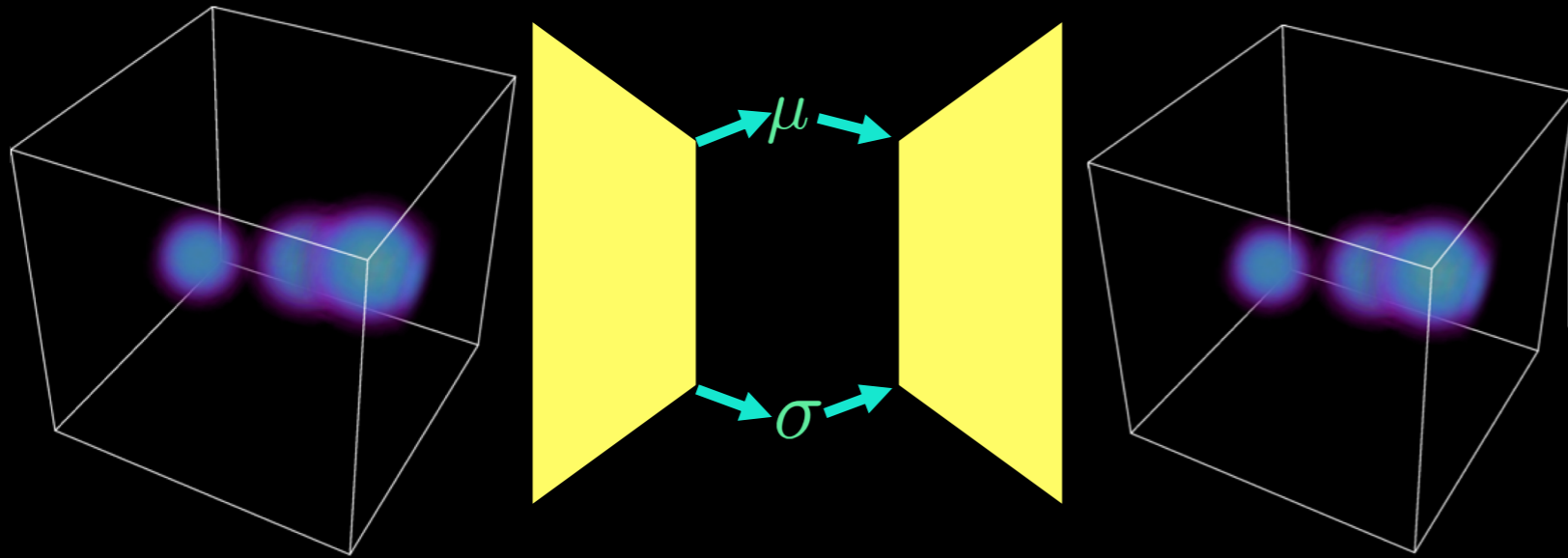
# Variational Autoencoder



# U-Net

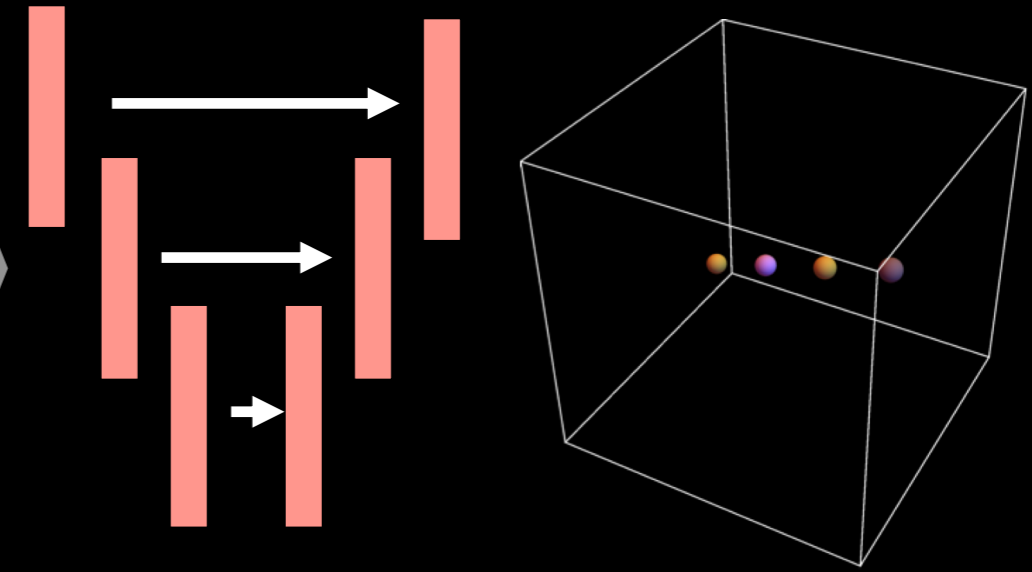


# Variational Autoencoder



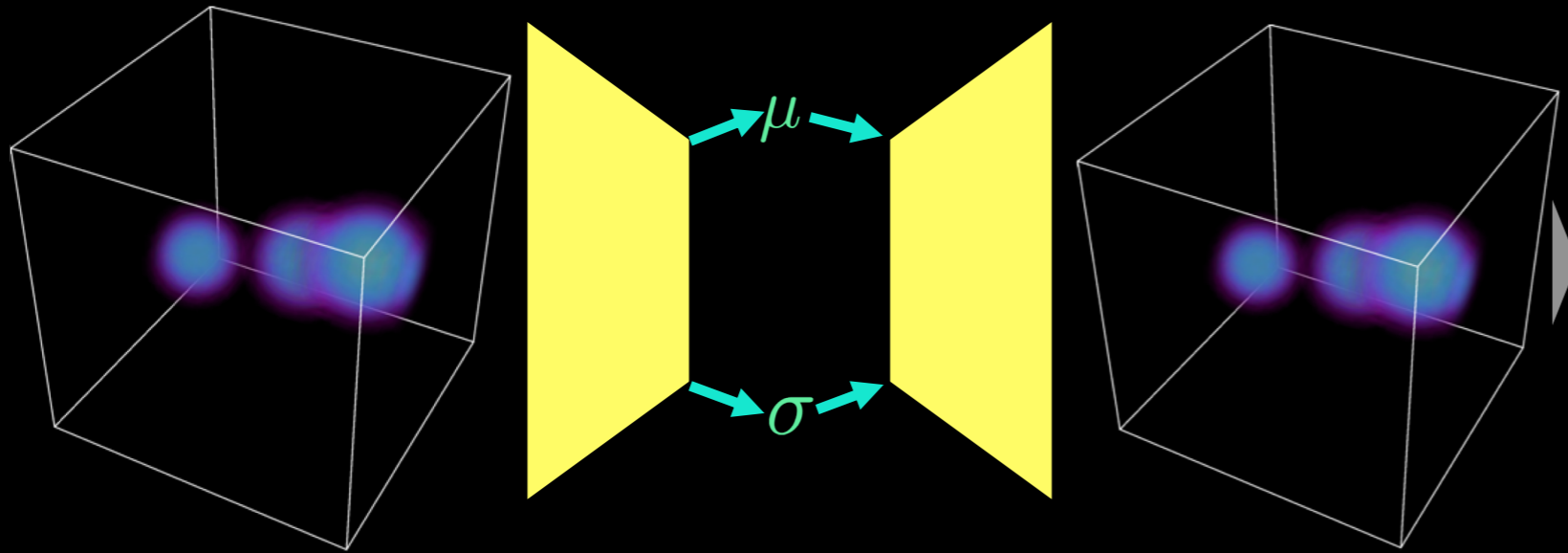
Encodes and decodes the density matrix.

# U-Net

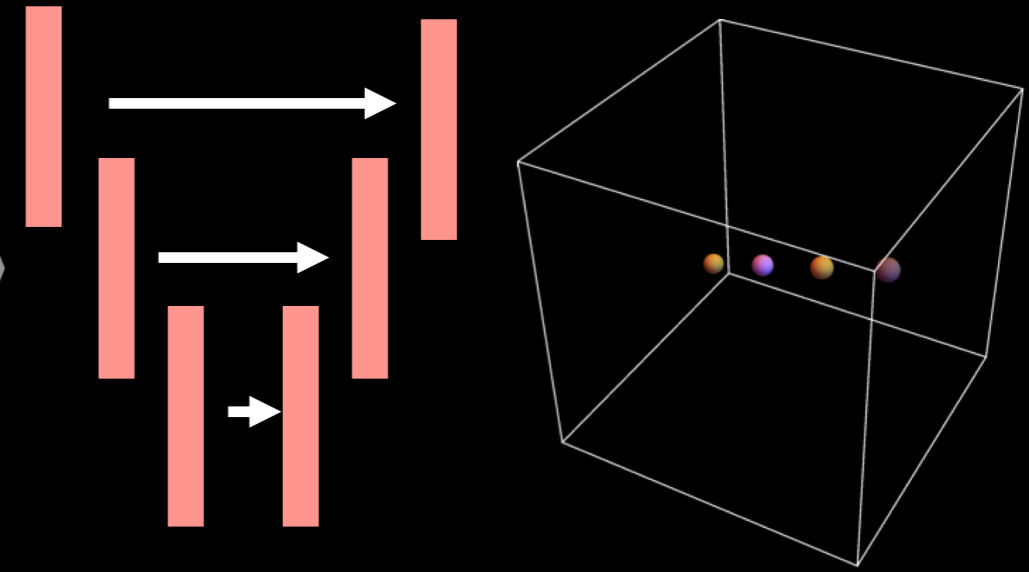


Solves the problem of converting a density field back to species. If  $\sigma = 0$ , trivial task. In theory, this is just solving a complicated optimization problem.

# Variational Autoencoder



# U-Net

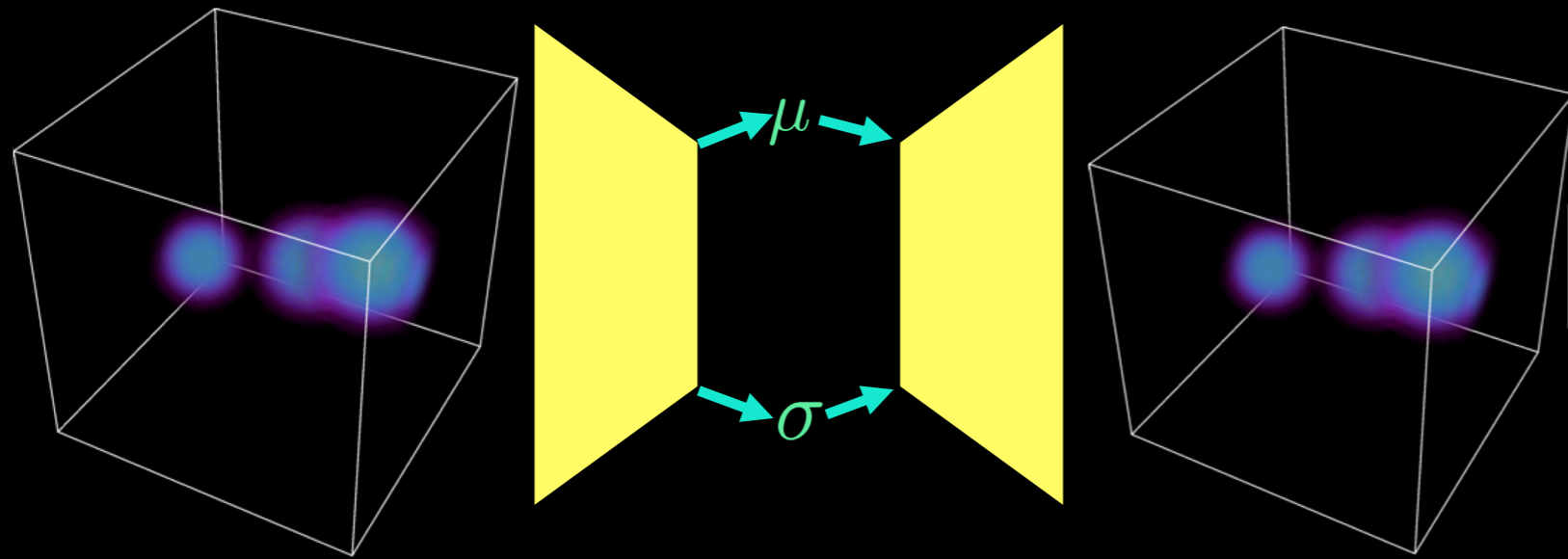


$$\mathcal{L}_{\text{VAE}} = L_{\text{RE}}(\hat{\mathbf{M}}, \mathbf{M}) + \beta(D_{\text{KL}}(q(\mathbf{z}|\mathbf{M})||p(\mathbf{z}))) + \gamma L_{\text{BCE}}(\hat{\mathbf{S}}, \mathbf{S})$$

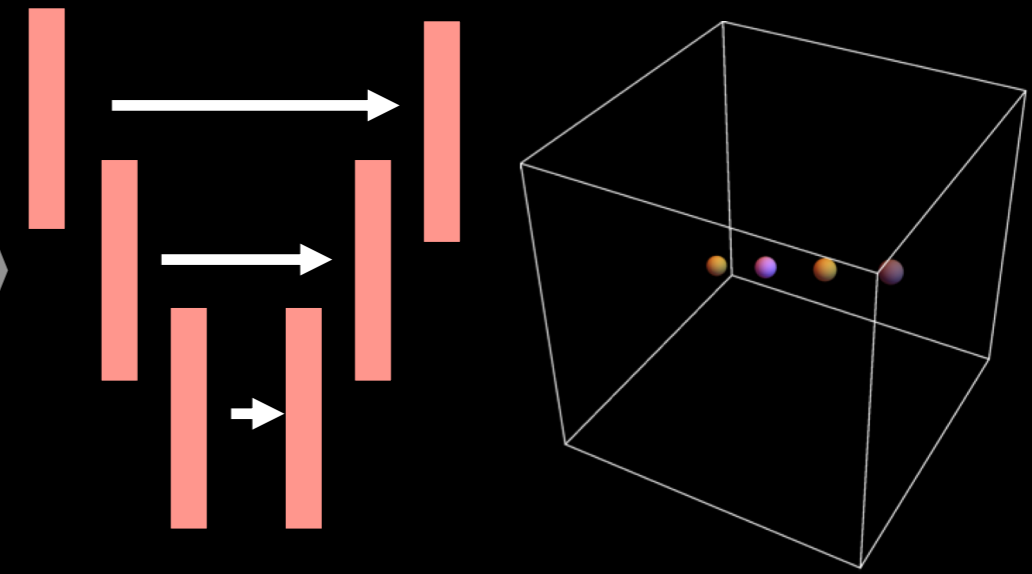
$$\mathcal{L}_{\text{U-Net}} = L_{\text{BCE}}(\hat{\mathbf{S}}, \mathbf{S})$$



## Variational Autoencoder

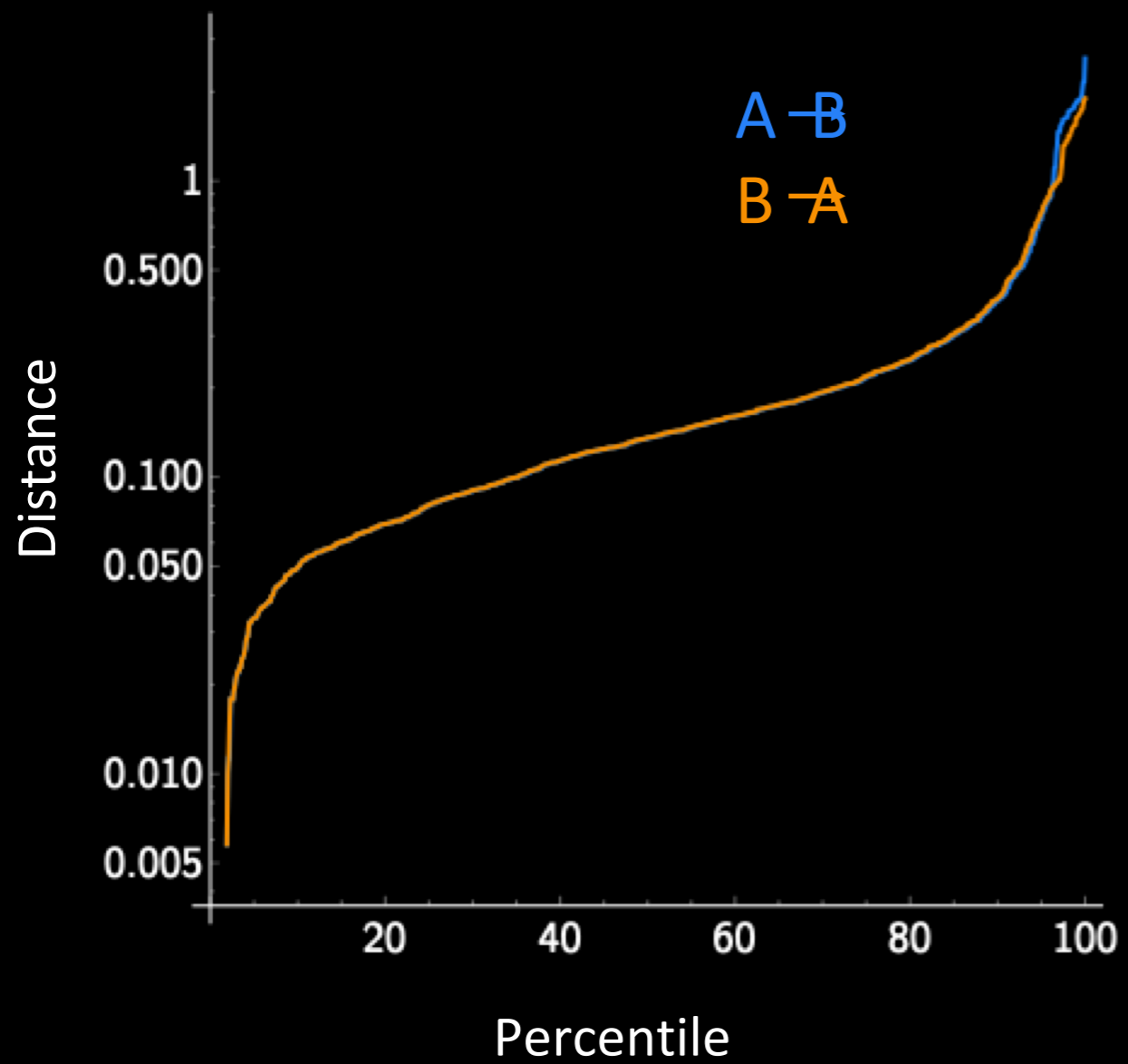


## U-Net

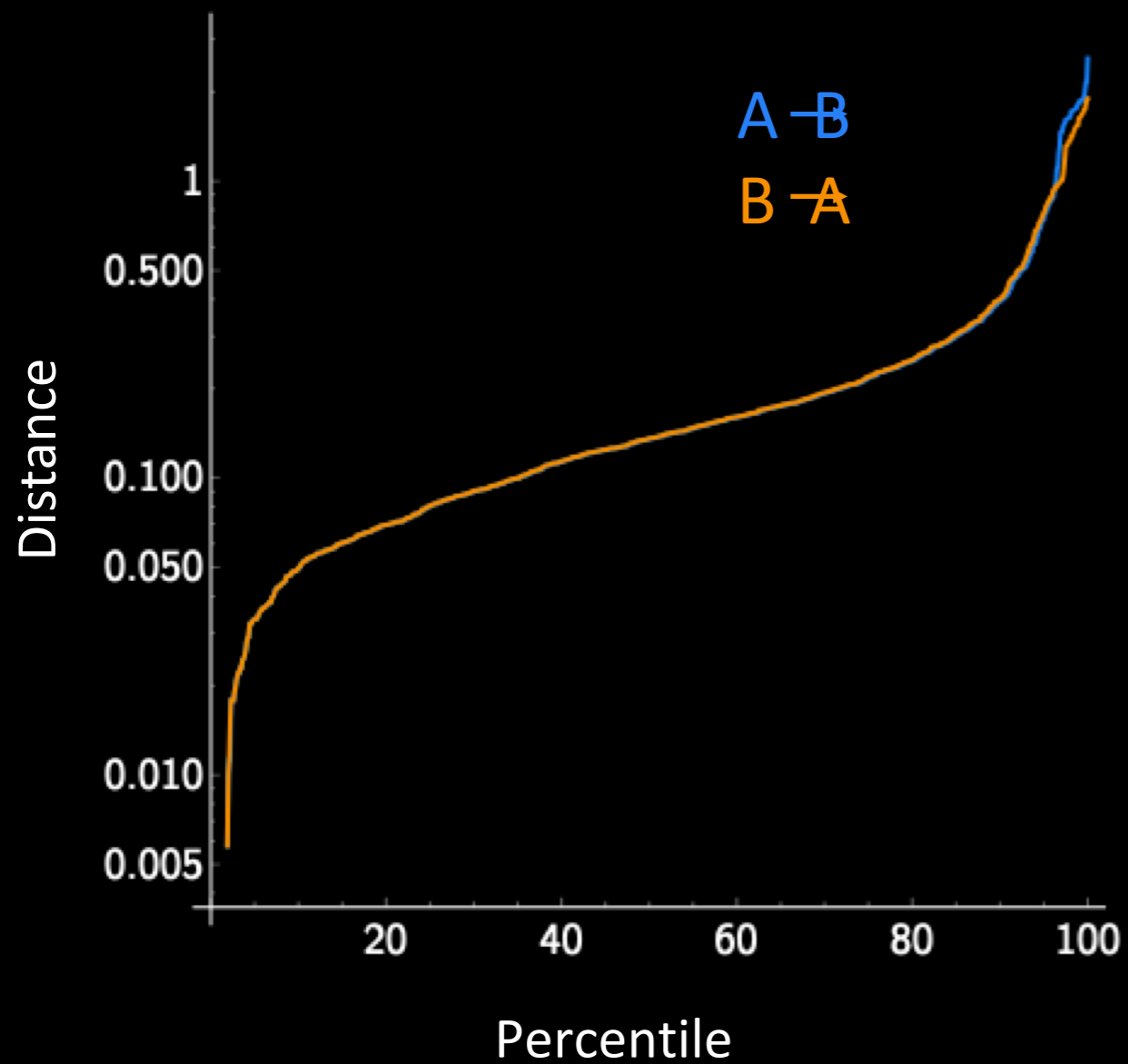


- 10 Angstrom on a side, used 30 and 60 pixels across
- 46,000 crystal structures, 35,000 considered
- Always centered, but we can rotate them randomly

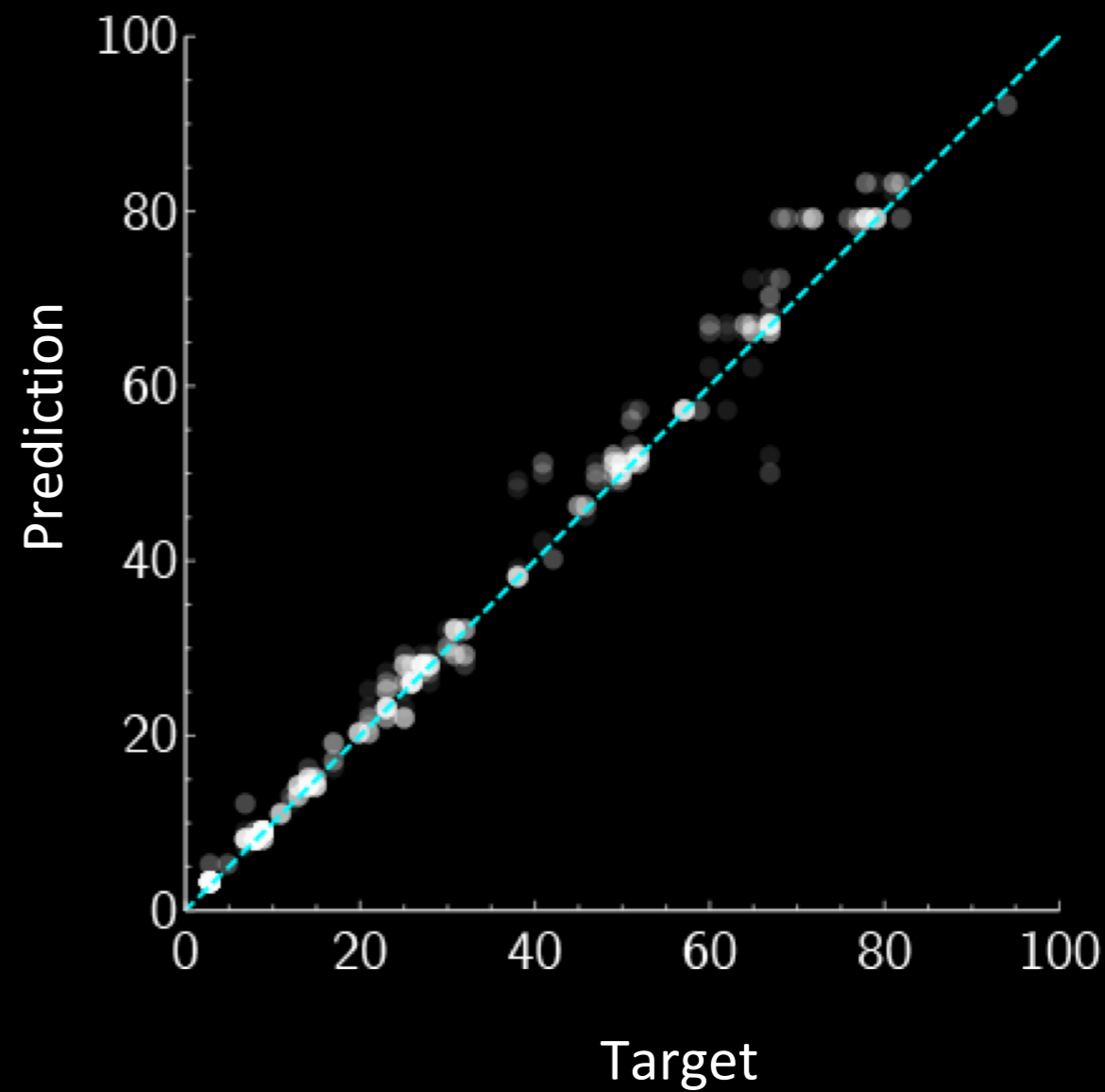
# Location Prediction



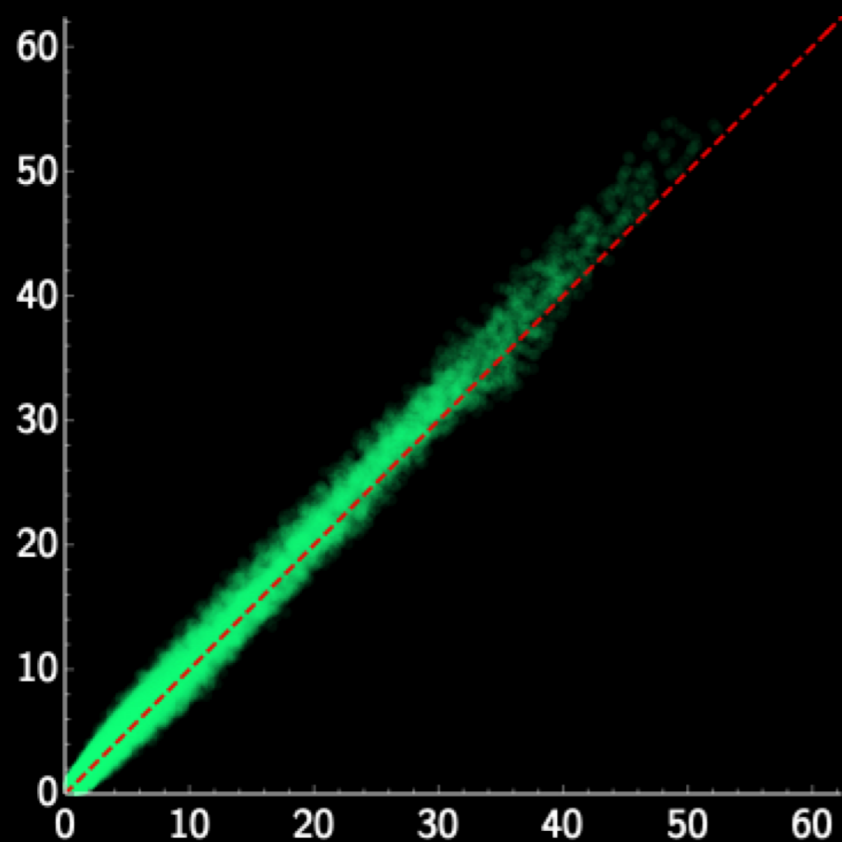
Location Prediction



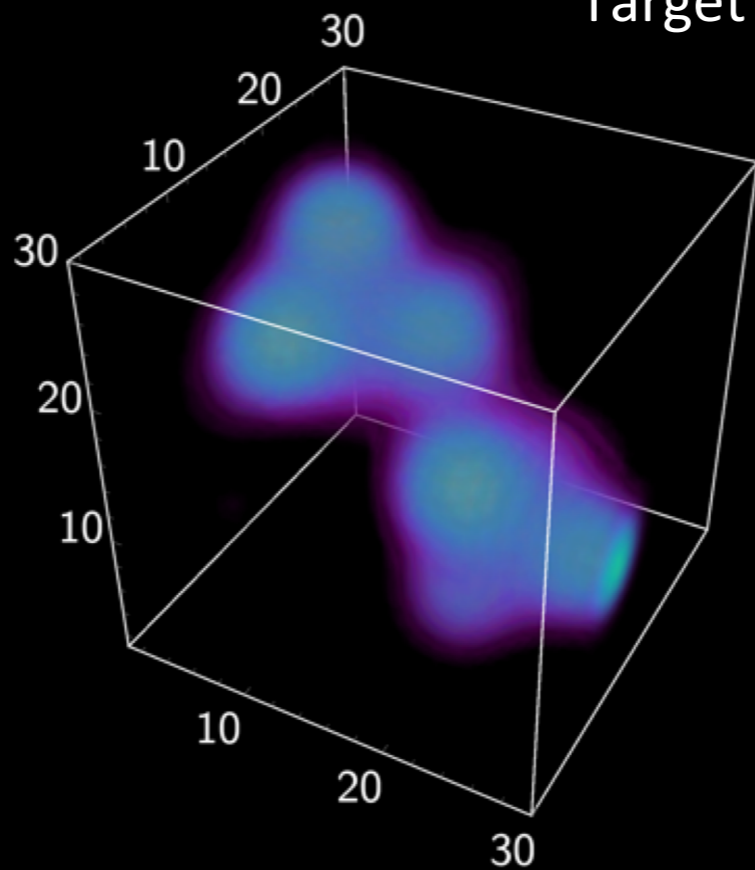
Species Prediction



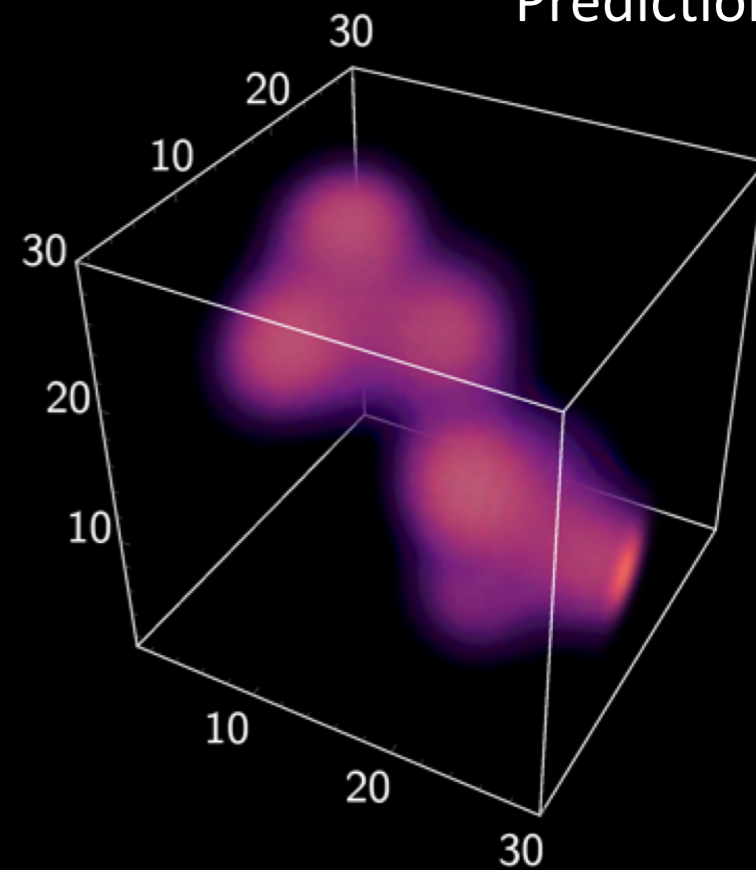
Prediction



Target

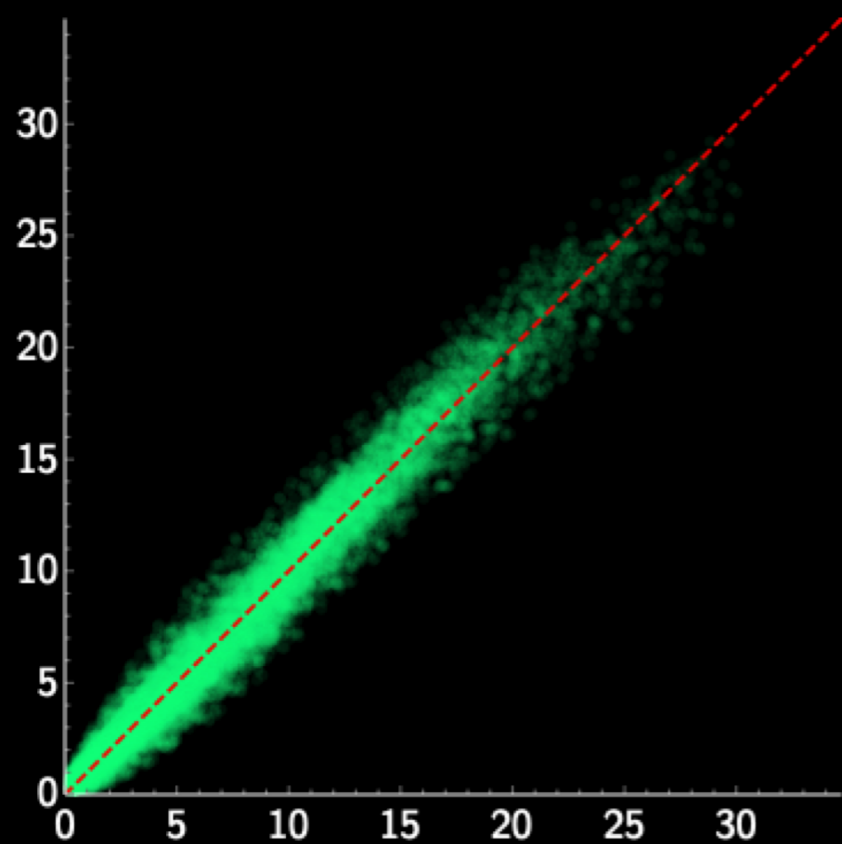


Prediction

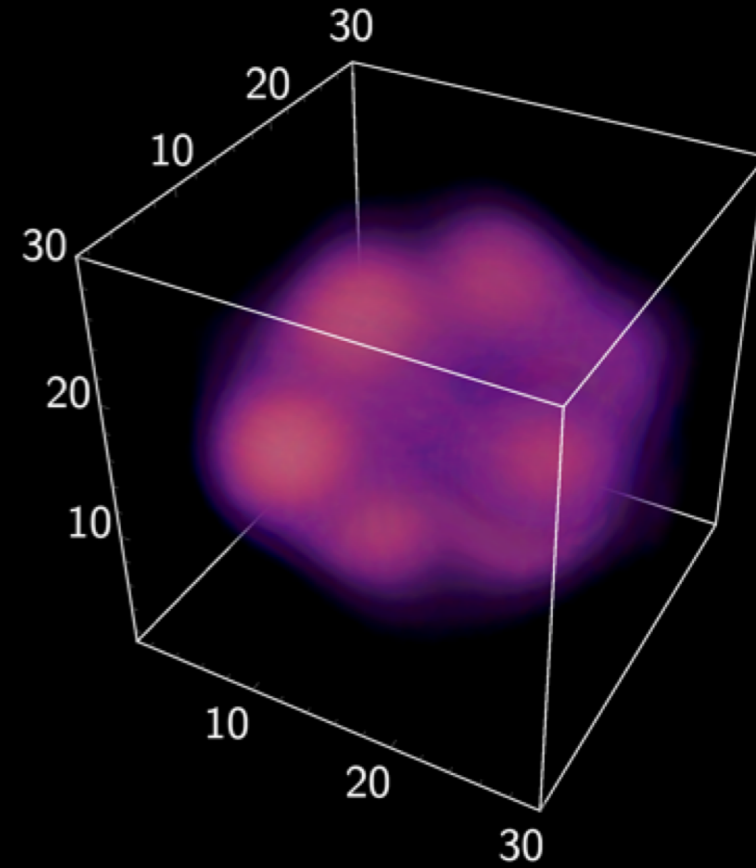
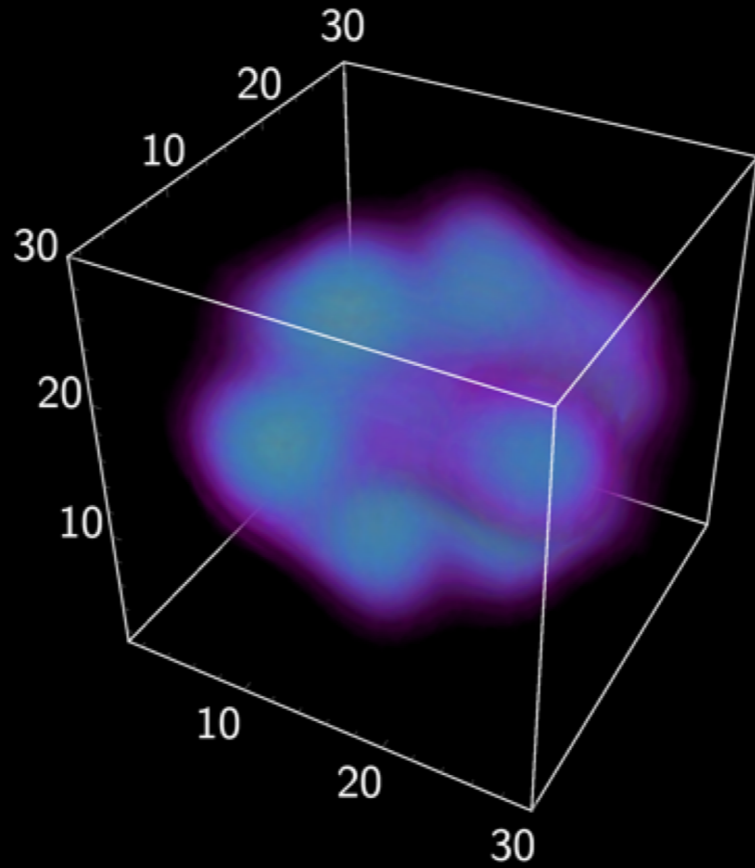


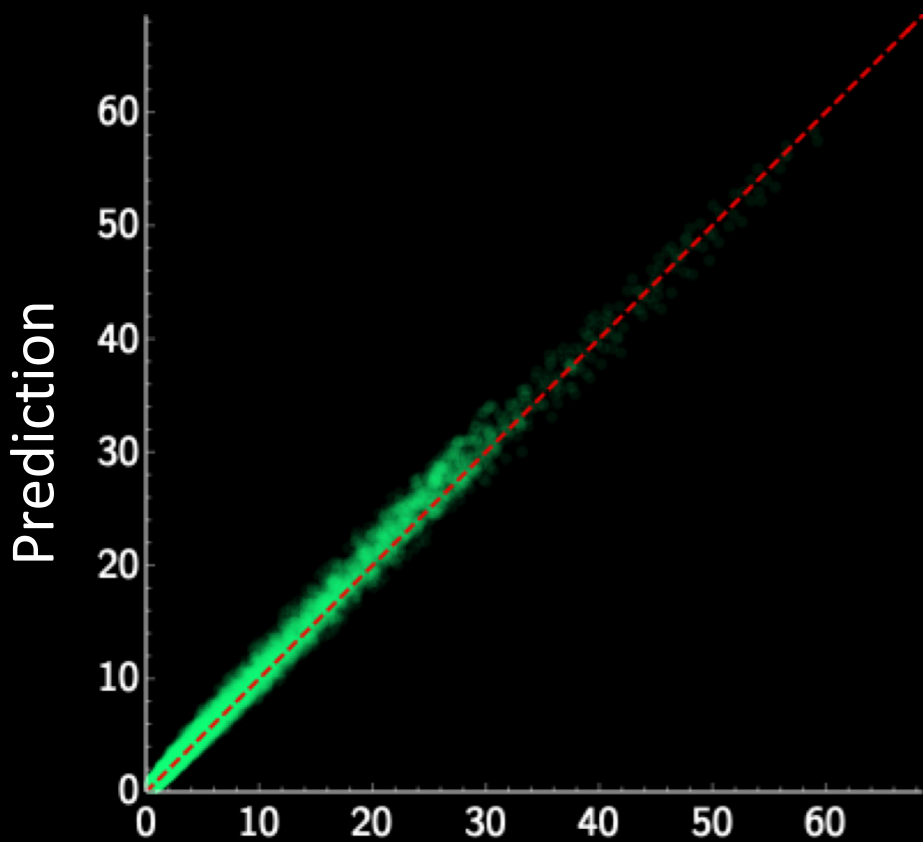
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Prediction

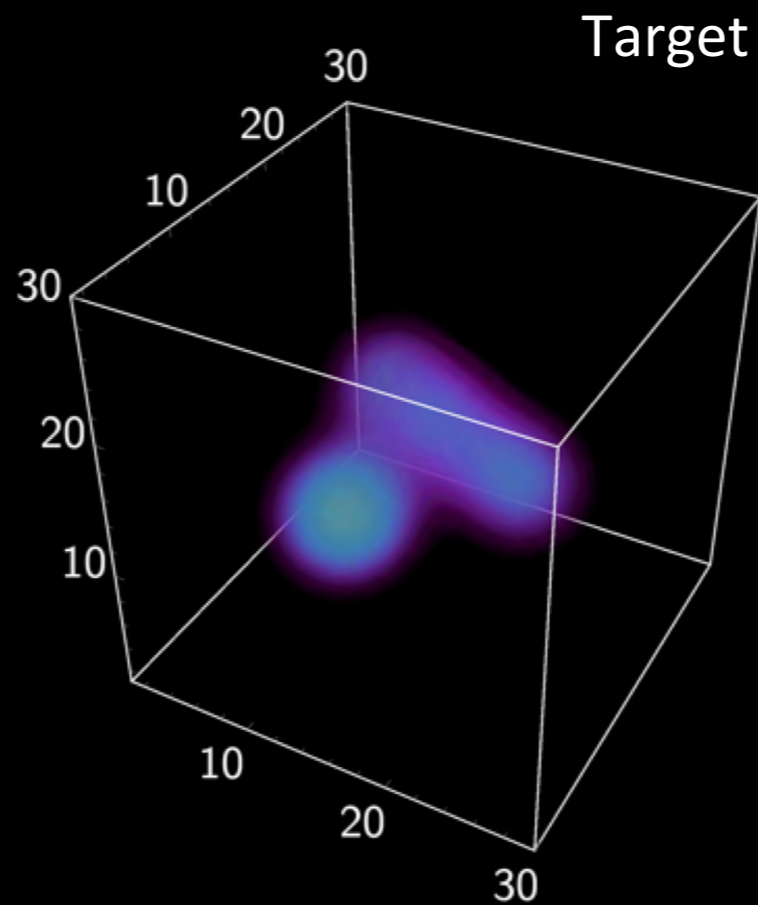


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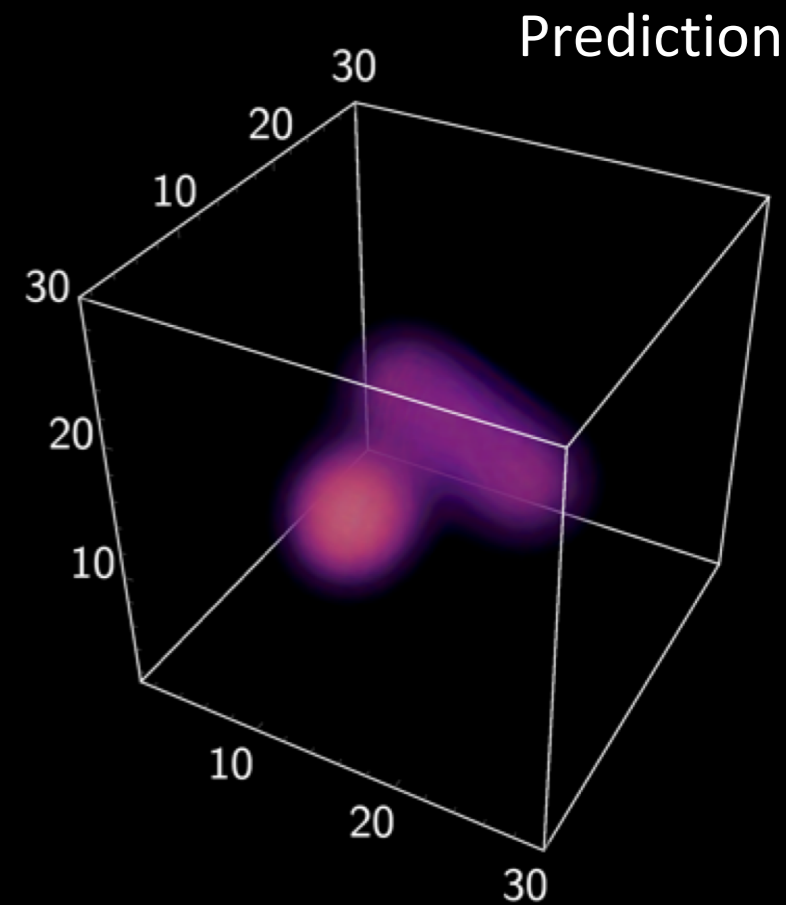




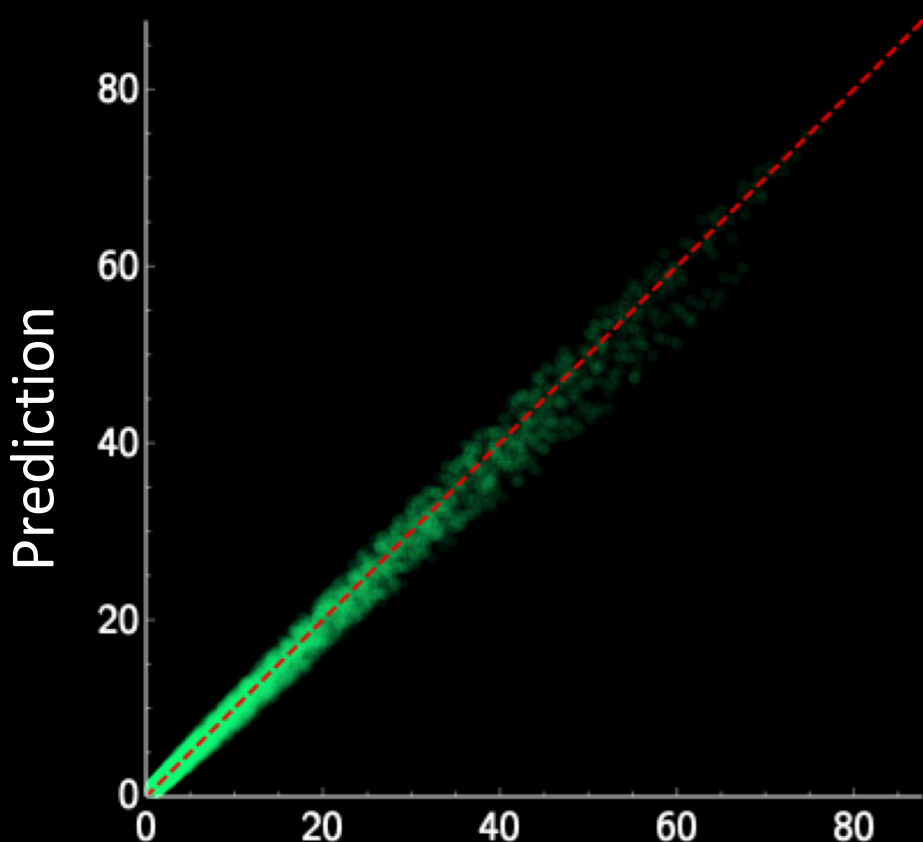
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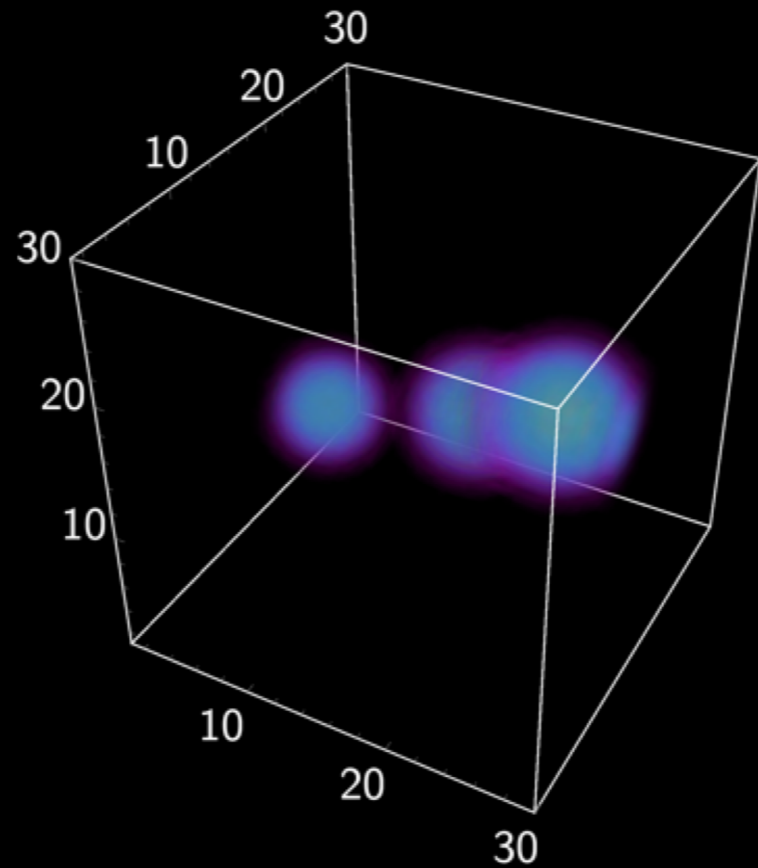
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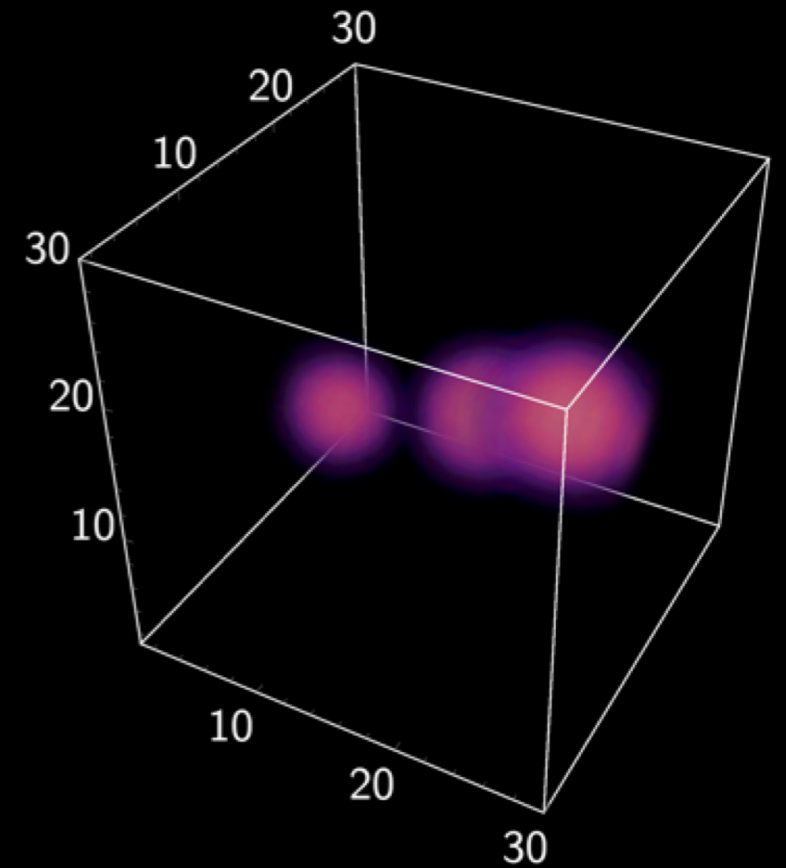
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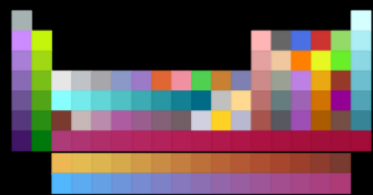
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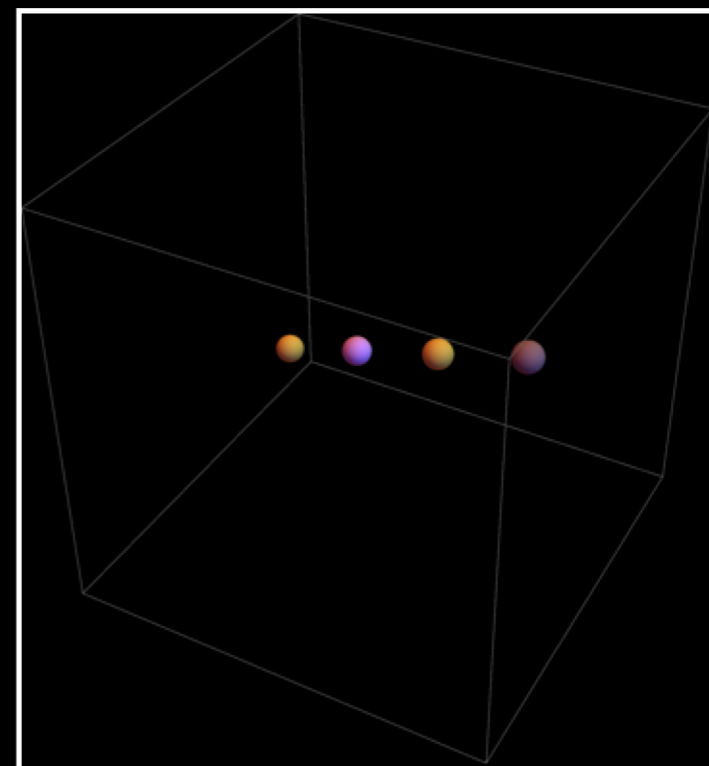
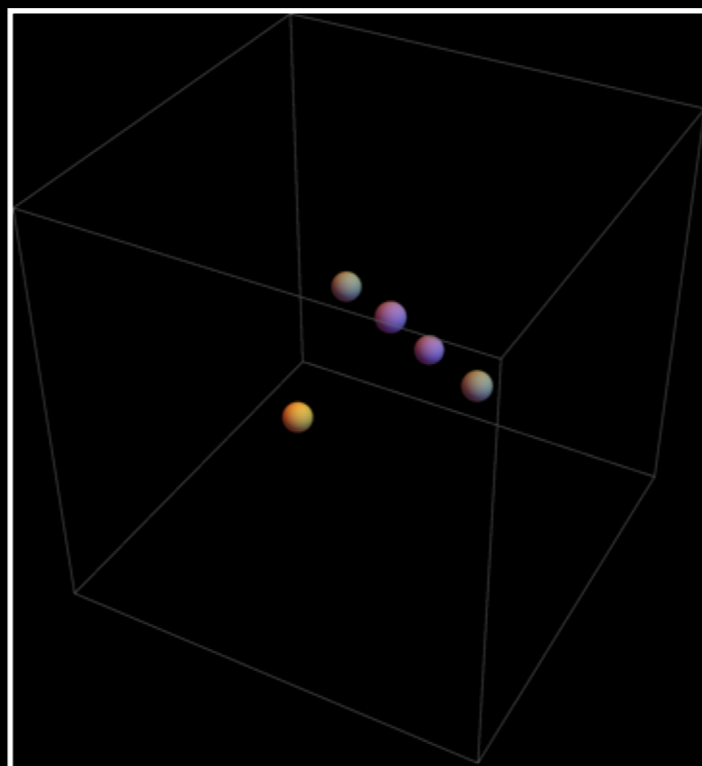
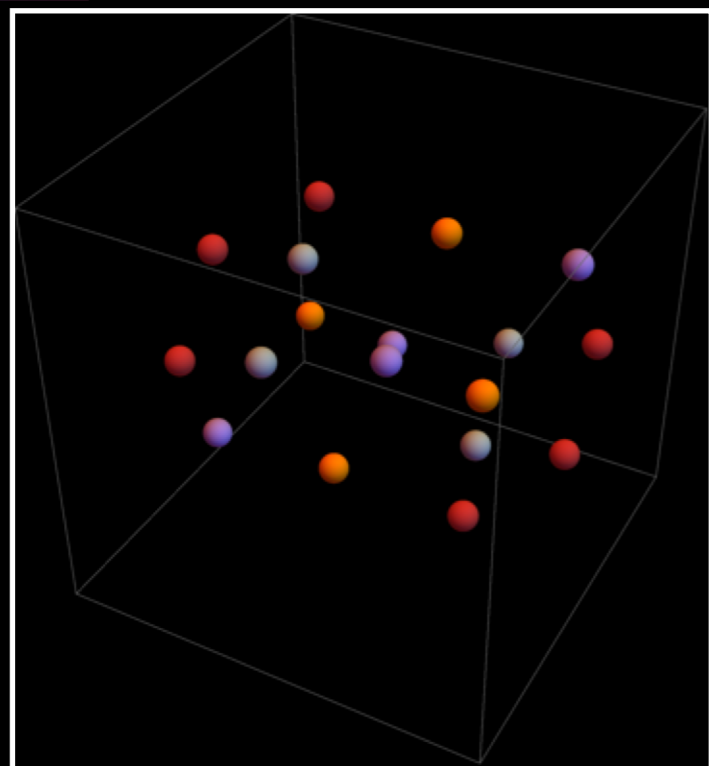
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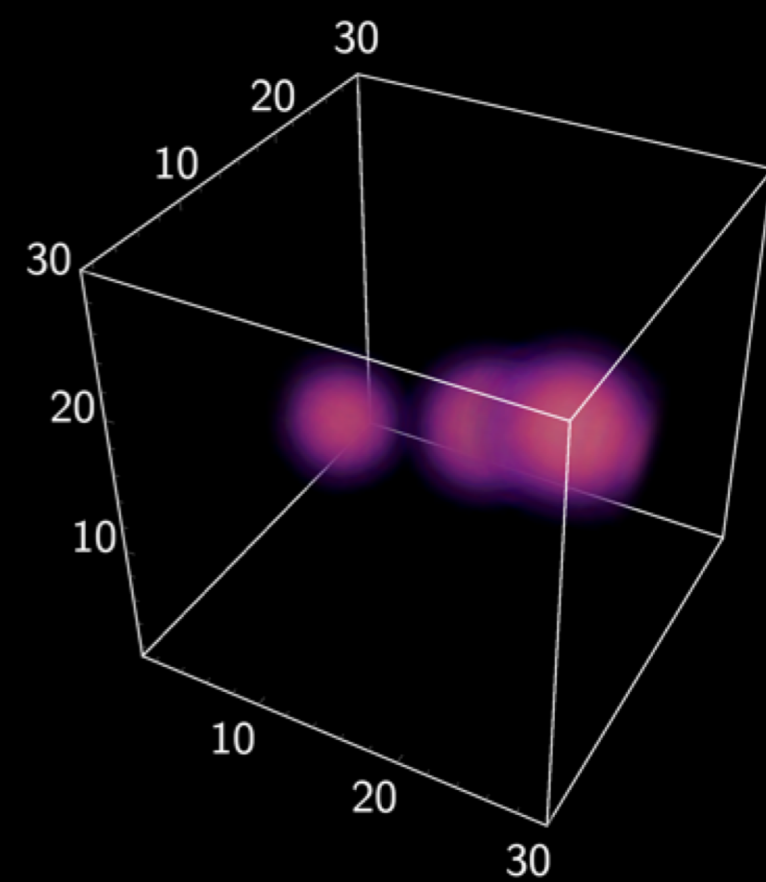
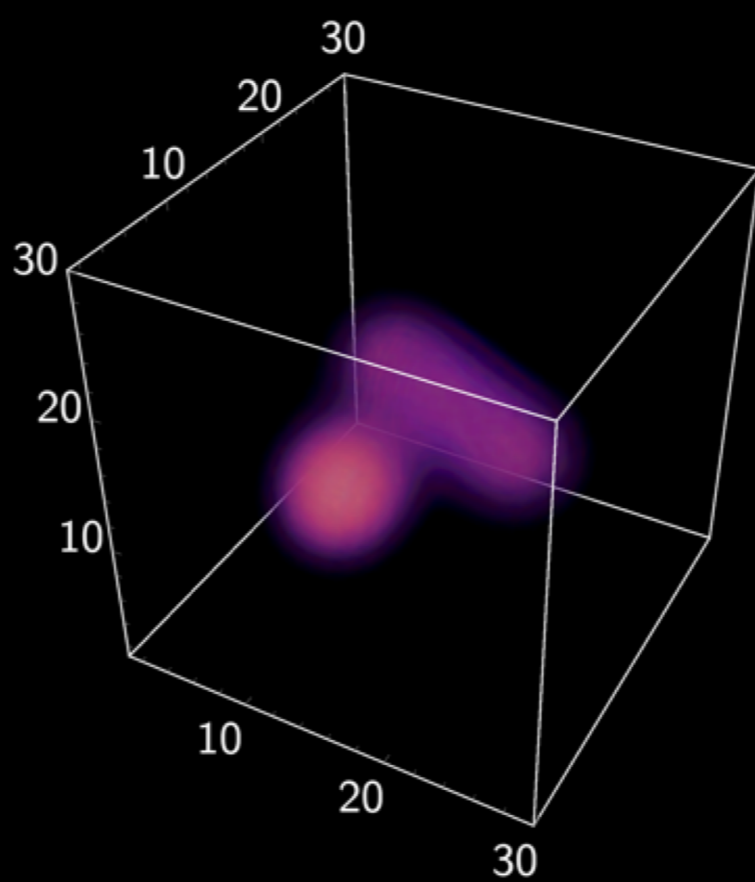
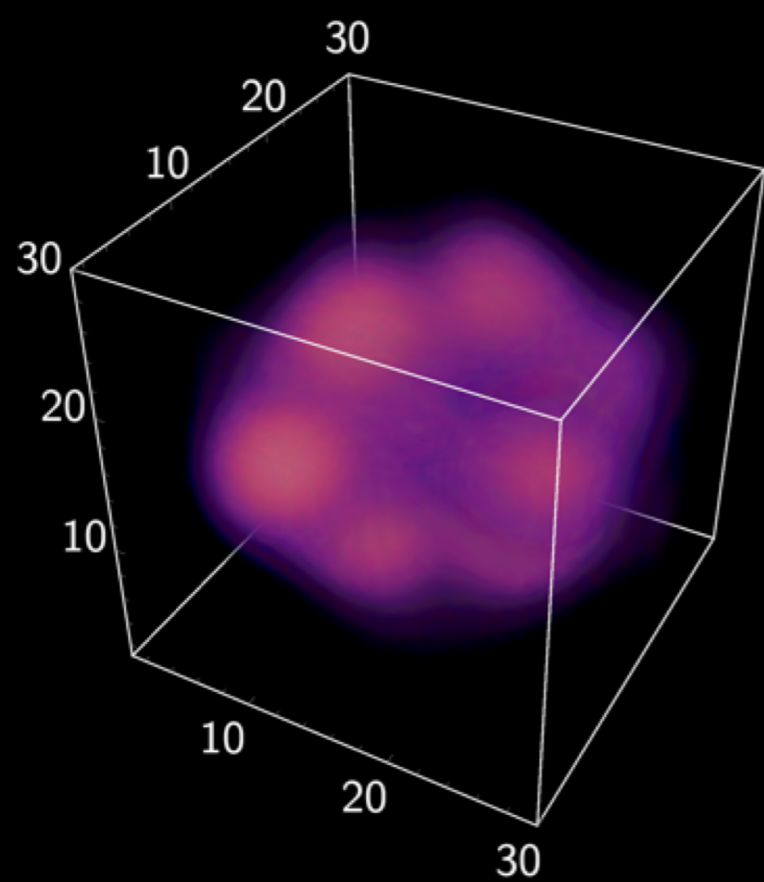
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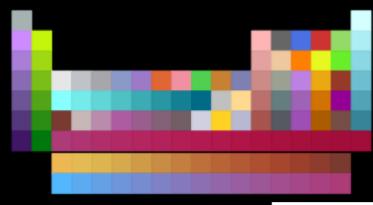


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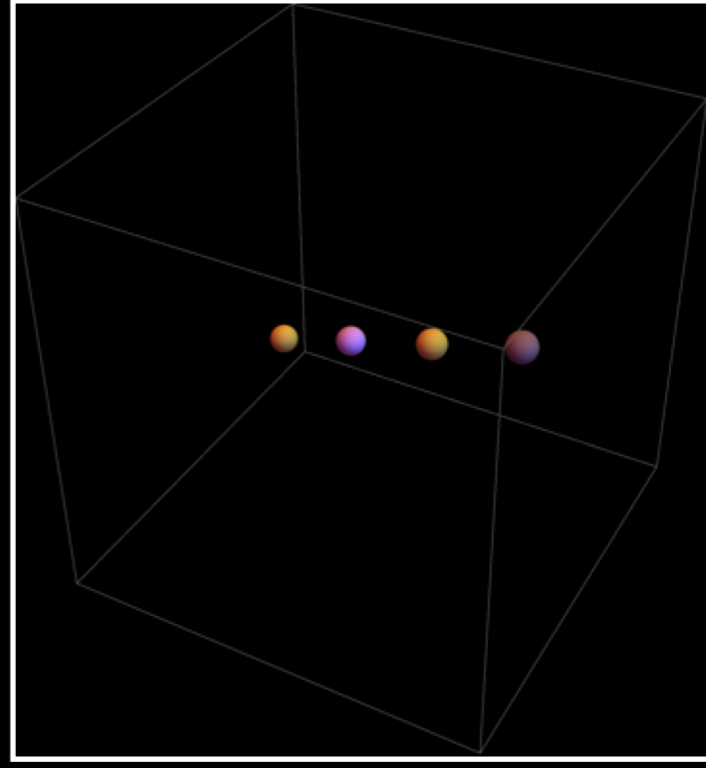
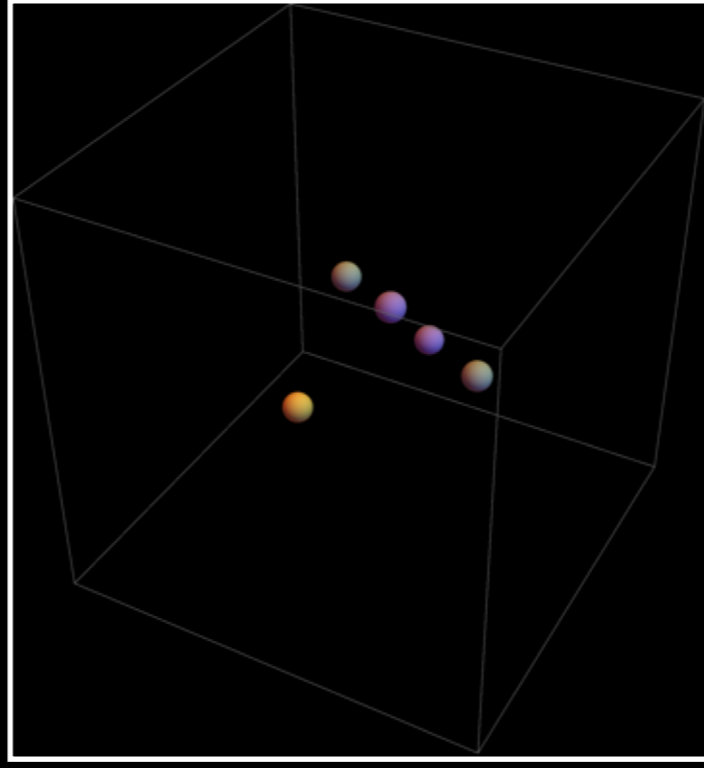
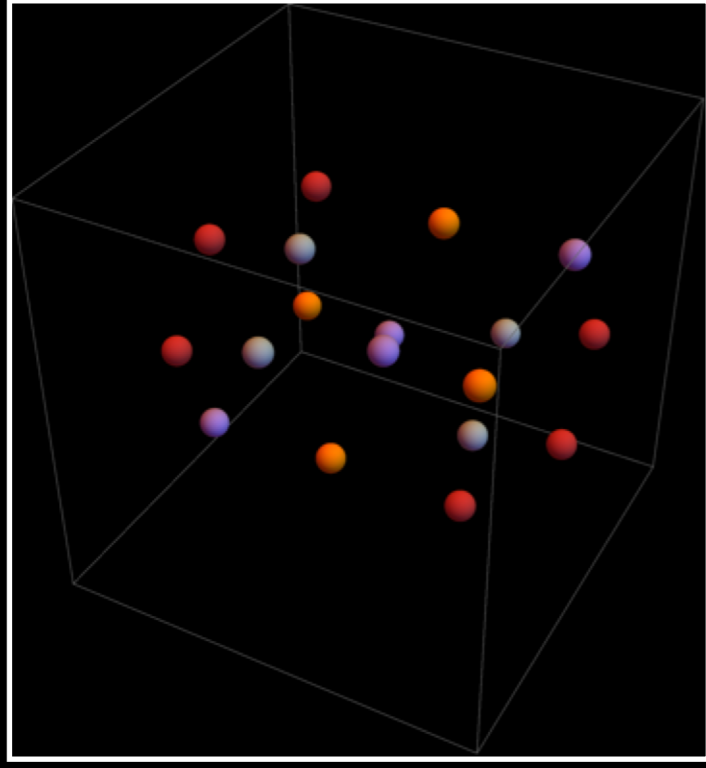


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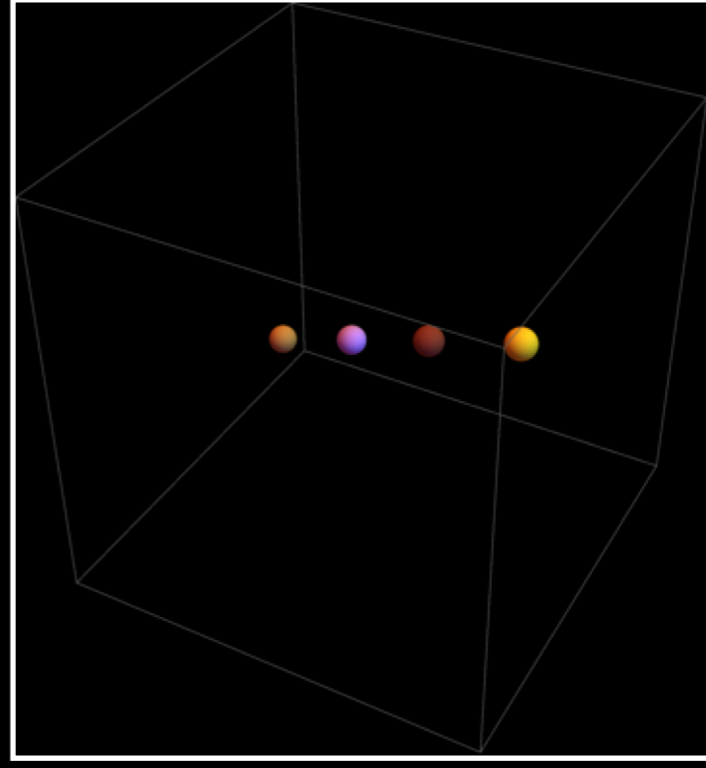
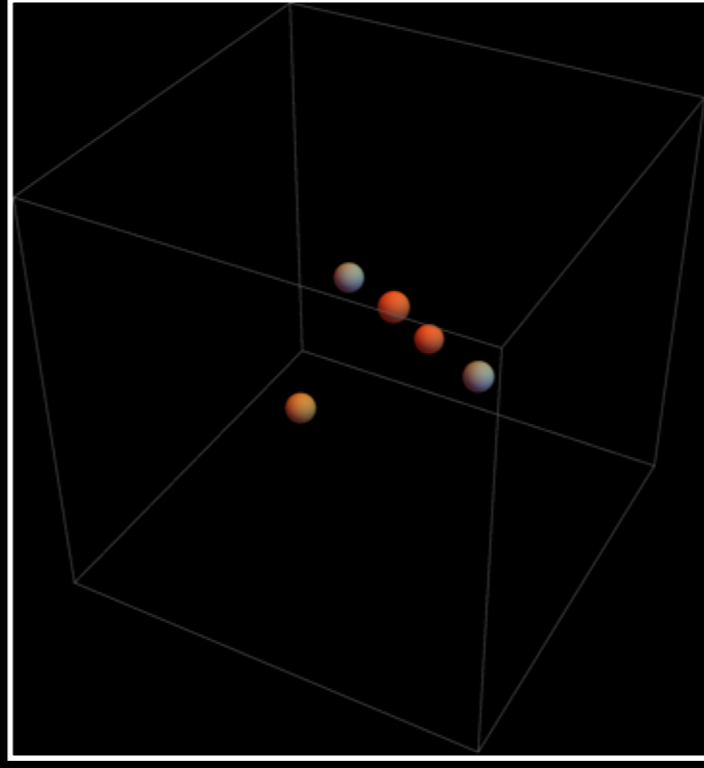
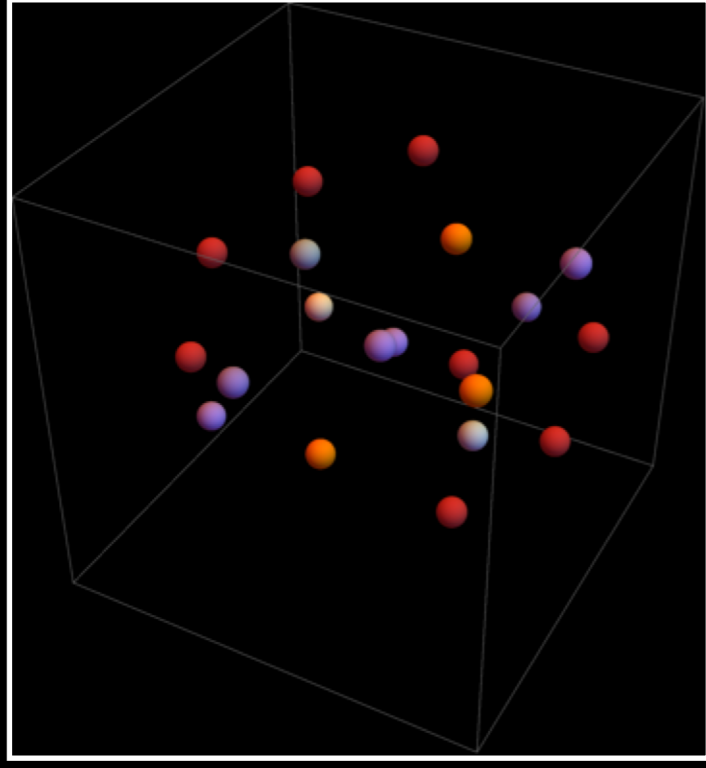




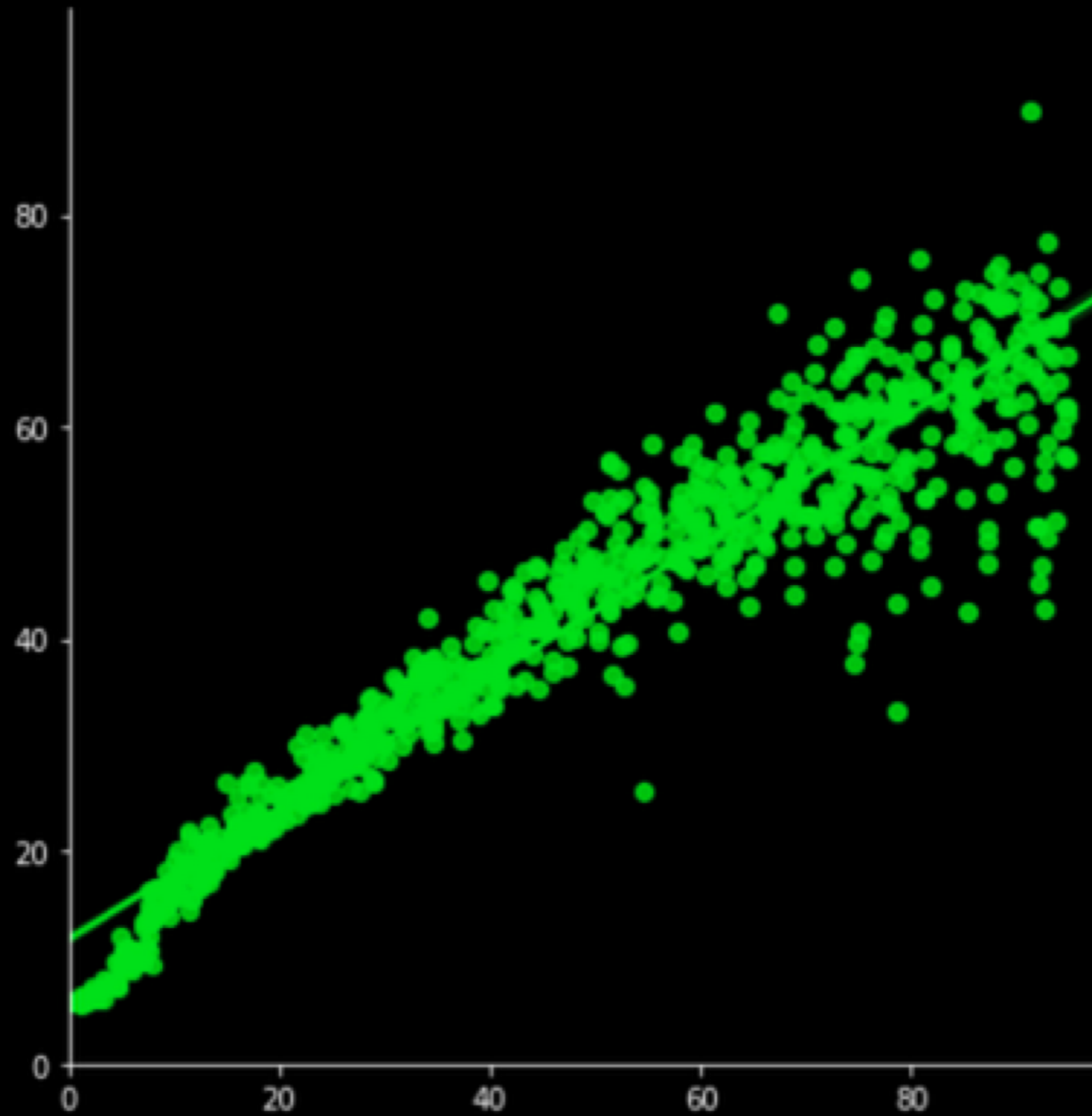
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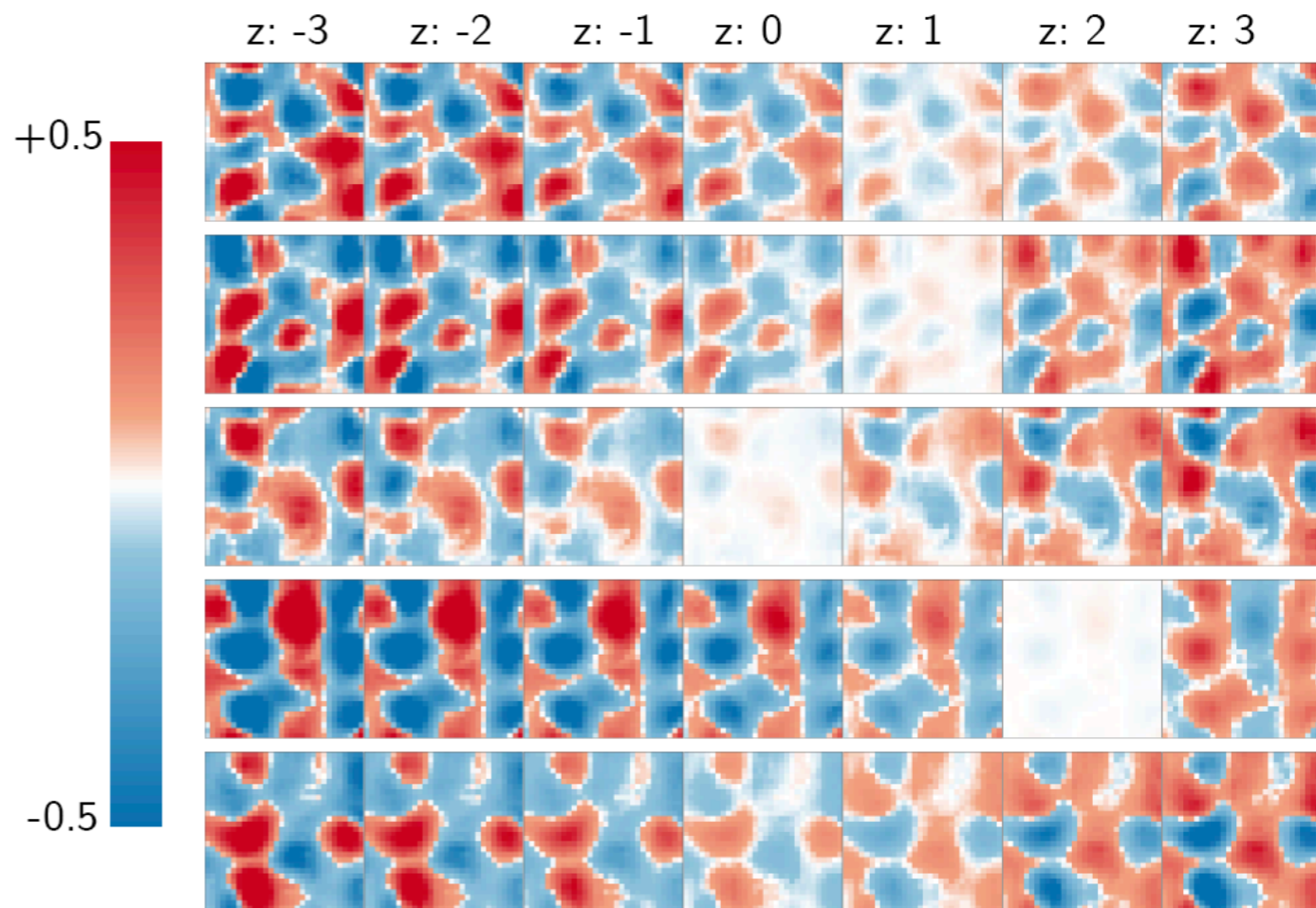
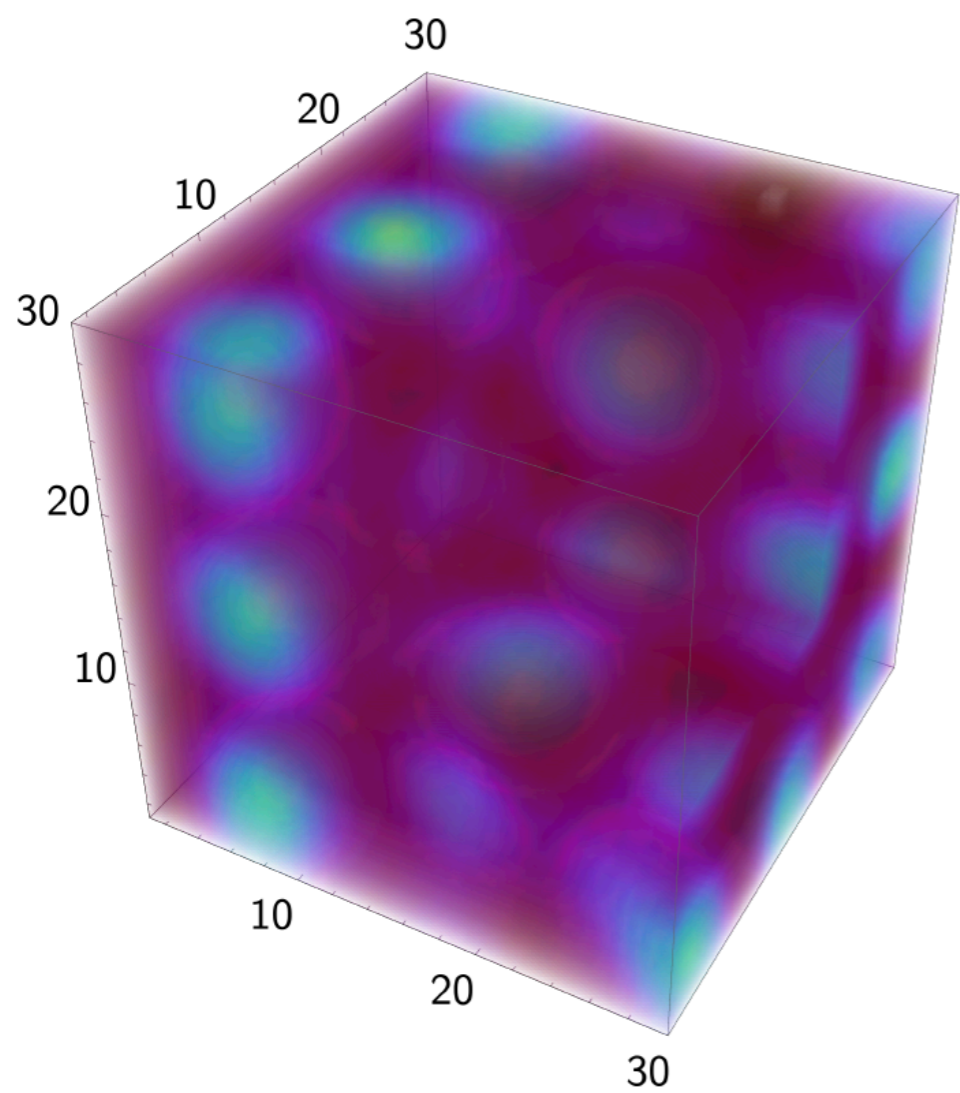
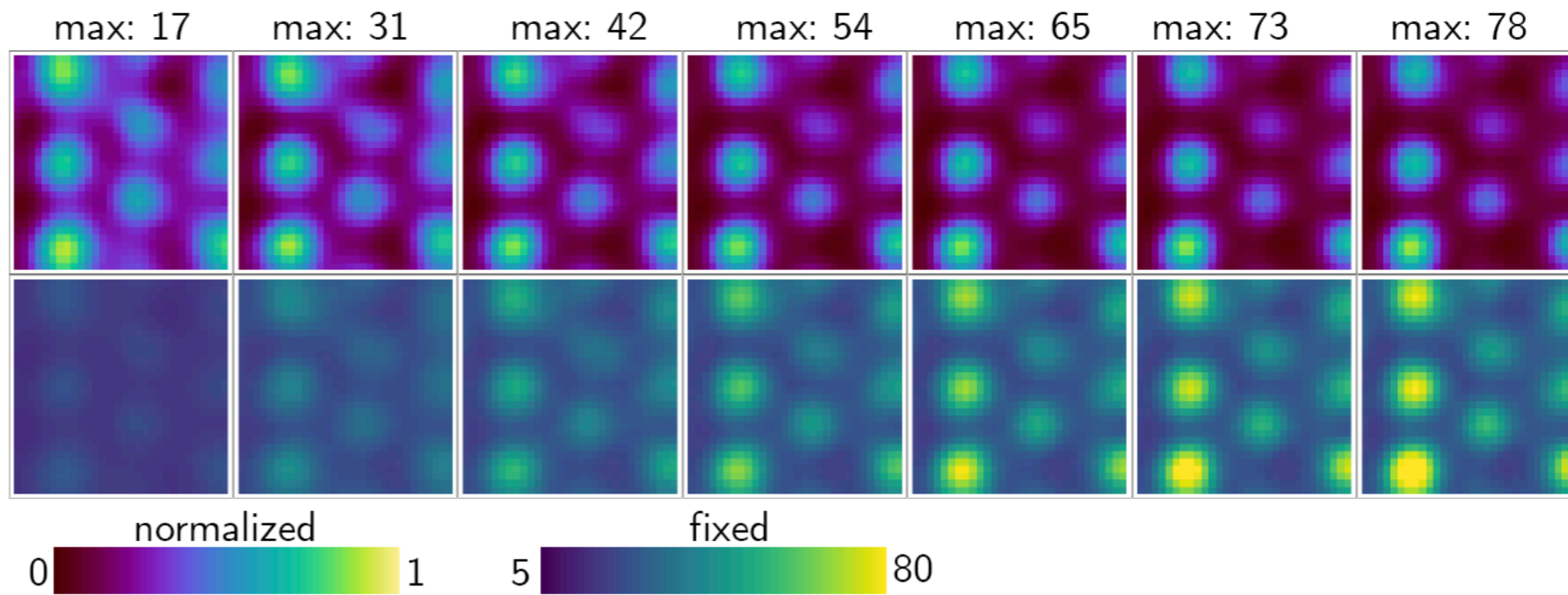
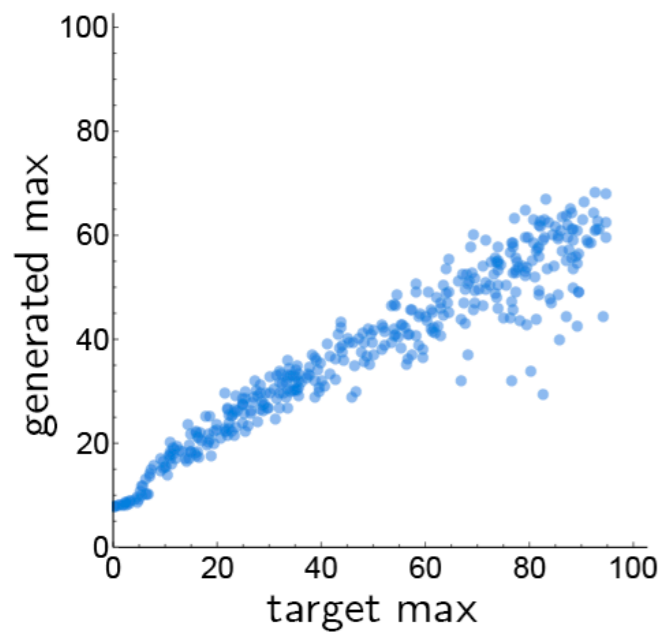


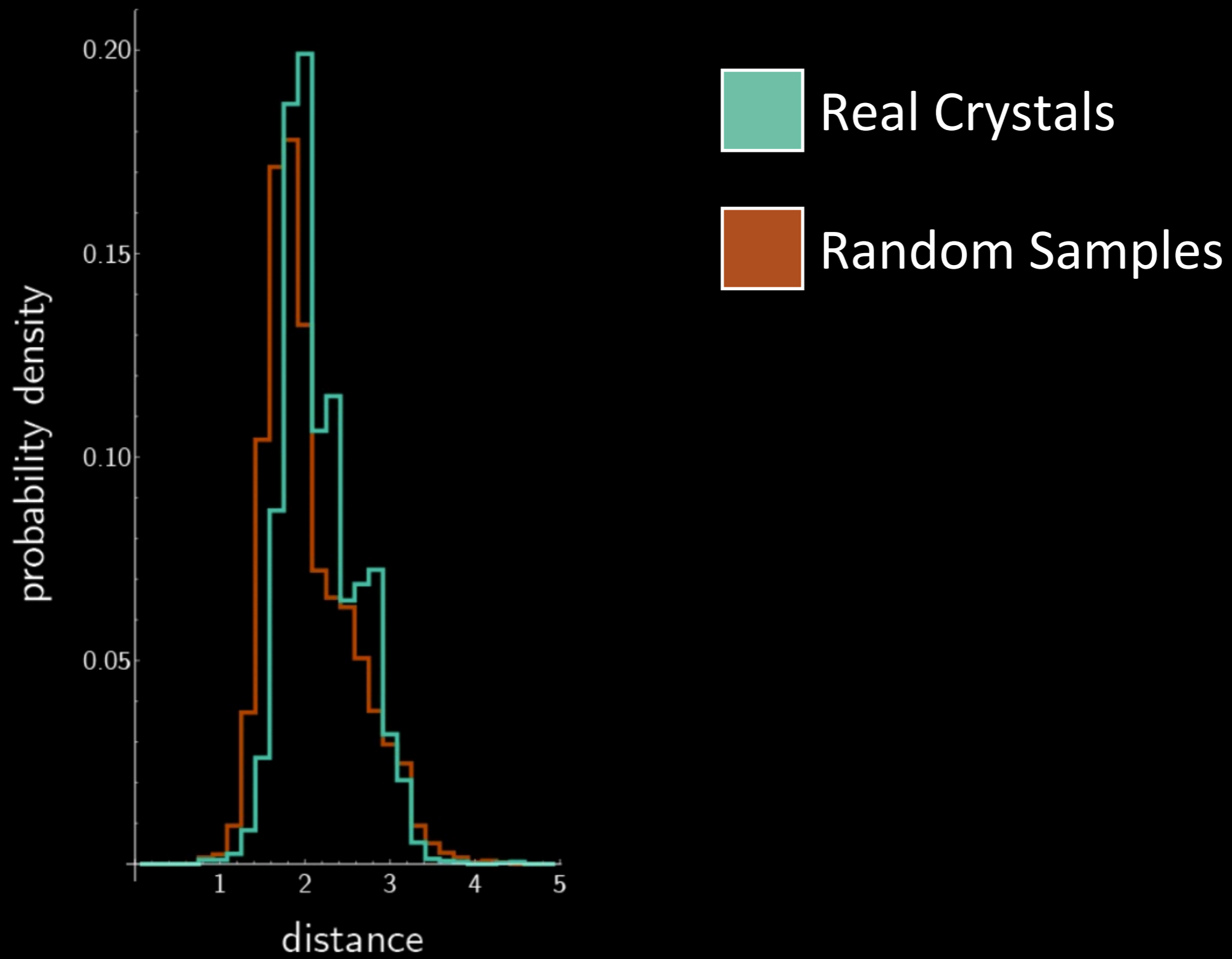
Generated largest electron density



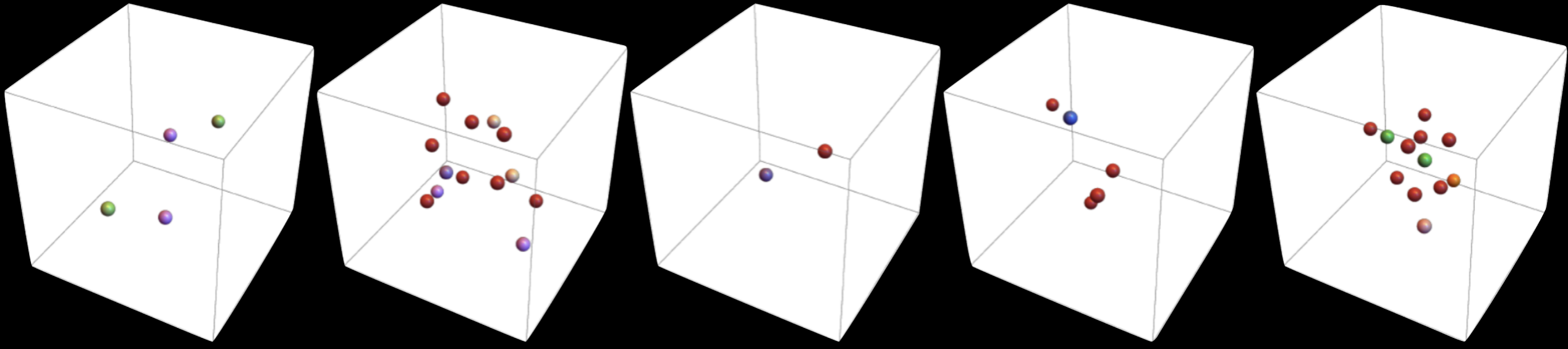
Target largest electron density



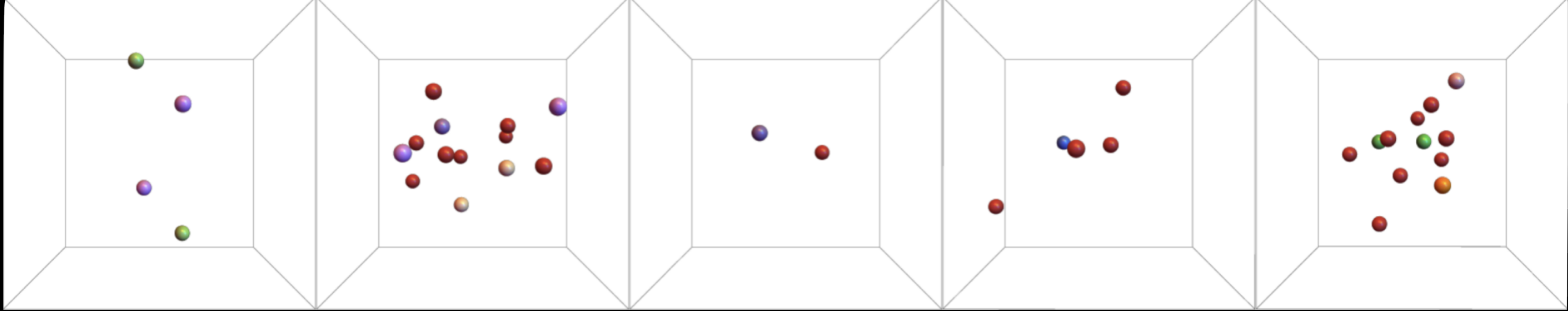




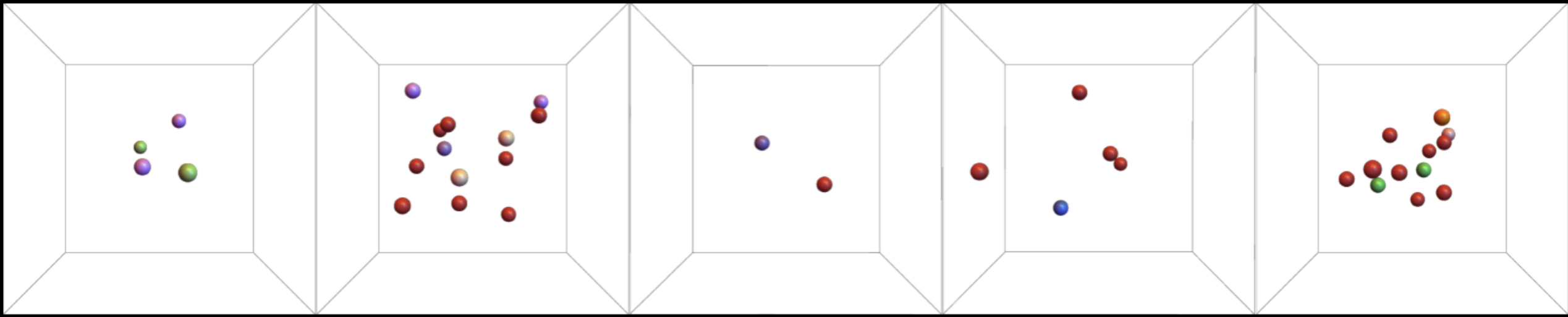
Atoms



Top view



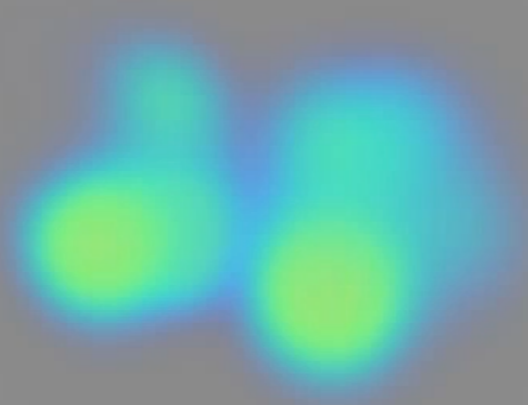
Front view



Scaled Density



Unscaled Density



Atoms

